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# How to find a Higgs Boson with a Mass between 155–180 GeV at the LHC

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#### Abstract

We reconsider the signature of events with two charged leptons and missing energy as a signal for the detection of the Standard Model Higgs boson in the mass region M(Higgs)=155-180 GeV. It is shown that a few simple experimental criteria allow to distinguish events originating from the Higgs boson decaying to  $H \to W^+W^-$  from the non resonant production of  $W^+W^-X$  at the LHC. With this set of cuts, signal to background ratios of about one to one are obtained, allowing a 5-10  $\sigma$  detection with about 5  $fb^{-1}$  of luminosity. This corresponds to less than one year of running at the initial lower luminosity  $\mathcal{L}=10^{33}cm^{-2}s^{-1}$ . This is significantly better than for the hitherto considered Higgs detection mode  $H \to Z^0Z^{0*} \to 2\ell^+2\ell^-$ , where in this mass range about  $100 \ fb^{-1}$  of integrated luminosity are required for a 5  $\sigma$  signal.

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#### 1 Introduction

The Standard Model of elementary particle physics (SM) has been highly successful in explaining all experimental data [1]. With the recent discovery of the top quark [2], the Higgs boson is the only remaining missing piece, albeit an essential one. Within the SM, it provides the mechanism to dynamically break the electroweak symmetry and gives masses to the electroweak gauge bosons. The same mechanism gives masses to the spin 1/2 fermions such as the top quark and the electron. The Higgs is therefore essential for our understanding of mass. Furthermore, the theoretical structure of the Higgs sector in the SM is the main motivation for speculations on physics beyond the SM, e.g. supersymmetry or technicolour. The discovery of the Higgs boson and the determination of its couplings could possibly provide an essential clue to this new realm. The search for the Higgs boson is therefore considered to be the most important task for future collider physics.

With the present energy upgrade of the large electron positron collider, LEP2, at CERN, the Higgs boson can be discovered for  $M_H \leq 98$  GeV [3] ( $\sqrt{s} = 192$  GeV). For larger masses the Large Hadron Collider (LHC) to be built at CERN, is the most promising discovery machine. There, the Higgs boson search is usually split into three Higgs mass regions [4, 5, 6]

(i) 
$$90 \text{GeV} < M_H < 130 \text{ GeV},$$
  
(ii)  $130 \text{GeV} < M_H < 2 \cdot M_{Z^0},$   
(iii)  $2 \cdot M_{Z^0} < M_H < 800 \text{ GeV}.$ 

For the mass regions (i) and (iii), Higgs detection with large significance is possible by the observation of narrow mass peaks using the decays  $H \to \gamma\gamma$  and  $H \to Z^0Z^0 \to 2\ell^+2\ell^-$  respectively [4, 5, 6]. For most of the mass region (ii) previous experimental studies, assuming excellent energy and momentum measurements of electrons and muons, have obtained promising mass peaks from the channel  $H \to Z^0Z^{*0} \to 2\ell^+2\ell^-$ , despite the low branching ratios [4, 5, 6]. However, the mass range between  $\approx 155-180$  GeV remains 1 difficult to detect because the Higgs decays almost exclusively to a pair of on shell  $W^{\pm}$ 's [4, 5, 6, 7, 8]. Consequently, a large integrated luminosity of about 100 fb<sup>-1</sup> is required for the Higgs detection using this four charged lepton signature.

In this letter we focus exclusively on the hitherto difficult mass region (ii) with

$$155 \text{ GeV} < M_H < 180 \text{ GeV}.$$
 (2)

We show that despite the absence of a narrow mass peak the decay

$$H \to W^+W^- \to (\ell^+\nu)(\ell^{\prime-}\bar{\nu}), \qquad \ell, \ell^{\prime} = e, \mu, \tau(\to \ell\nu\bar{\nu}),$$
 (3)

provides a straight forward discovery channel, especially in this mass range.

2 
$$\mathbf{H} \to \mathbf{W}^+ \mathbf{W}^- \to (\ell^+ \nu)(\ell'^- \bar{\nu})$$

The Higgs decay to two W-bosons as well as the branching ratio, was first calculated in Ref.[9] at tree-level. The one-loop result was obtained shortly thereafter [10]. In the mass range (2) the Higgs decay to two  $W^{\pm}$  bosons is dominant with a branching ratio close to unity. For  $W^{\pm}$ and  $Z^0$  boson decays, isolated high  $p_t$  electrons and muons are typically clean and detectable signs of events. Despite the larger branching ratios, the identification of  $W^{\pm}$  and  $Z^{0}$  using the decays into jets is difficult to distinguish from the abundant jet background at the LHC even if one (W, Z) decays leptonically [11]. We therefore consider only the leptonic final states,

$$W^{\pm} \rightarrow \ell^{\pm}\nu_{\ell}, \qquad \ell = e, \mu, \tag{4}$$

$$W^{\pm} \rightarrow \tau^{\pm}\nu_{\tau} \rightarrow \ell^{\pm}\nu_{\ell}\nu_{\tau}. \tag{5}$$

$$W^{\pm} \rightarrow \tau^{\pm}\nu_{\tau} \rightarrow \ell^{\pm}\nu_{\ell}\nu_{\tau}. \tag{5}$$

As a result, about 7% of all W-pair events will have two oppositely charged leptons  $(e, \mu)$  [12] and at least two neutrinos resulting in a considerable missing transverse momentum imbalance. This should be compared to the gold plated Higgs decay signature into two Z bosons followed by their leptonic decays. While the latter channel provides a narrow mass peak, it suffers from the low Z branching ratio to electron and muon pairs with a four charged lepton branching ratio of less than 0.45% [12]. Combining this, with the factor of roughly 20-30 for the branching ratio of the Higgs to  $W^+W^-$  with respect to  $Z^{0*}Z^0$  in the mass range (2) [5, 6, 7, 8], we see that the decay signal (3) is more than two orders of magnitude above the gold plated signature. This large rate can therefore be expected to compensate for the absence of a narrow mass peak due to the two undetected neutrinos.

For an intermediate mass Higgs, the fully leptonic decay signature (3) was first studied by Glover et al. [13] for the LHC ( $\sqrt{s} = 16 \text{ TeV}$ ). They explicitly did not consider the background from  $t\bar{t}$  production and focused on the "irreducible" background from  $W^{\pm}$  pair production, for which they did not include any discriminating cuts. They concluded that the final state (3) should provide detectable Higgs signals at the LHC. Subsequently, Barger et al. [14] performed a more detailed parton level analysis of this signature for the LHC ( $\sqrt{s} = 16$  TeV). They went beyond [13] to include the significant  $t\bar{t}$  background for  $m_{top}=150,\,200$  GeV (the top quark mass was not yet known). Furthermore, in their study,  $W^{\pm}$ 's from signal and background are simulated only with their leptonic decays to  $e\nu$  and  $\mu\nu$ . They did not include the mode (5). Otherwise, their cuts are very similar to those in [13], in particular they also do not perform cuts to reduce the "irreducible" WW background. They again concluded, despite a much worse signal to background ratio, that this channel should provide a reasonable possibility to detect the Higgs in this mass range. However, they also point out that a more detailed study including hadronisation will eventually be necessary to substantiate the parton level results.

Since then this Higgs signal has been ignored as a discovery channel and the mass region between 155 GeV and 180 GeV has been identified as a problem area of the Higgs detection at the LHC [4, 5, 6]. The motivation of this study is to demonstrate that the potentially last Higgs-search gap at the LHC can be closed using the specific decay (3).

In the study described in the following, we go in many respects far beyond the previous theoretical studies [13, 14]. We have included the decay (5) in the signal and in the background. Furthermore we have included the background process<sup>1</sup>  $gg \to Wtb$ , which is of the same order as top pair production after the initial set of cuts. Most importantly, in all cases a full simulation of QCD processes including hadronisation processes is done using the PYTHIA Monte Carlo [15] with the default CTEQ2L set of structure functions.

We find that the cuts previously employed [13, 14] are then no longer sufficient. We have thus included new cuts in particular also to discriminate against the "irreducible"  $W^+W^-$  background. Furthermore, the criteria used to select signal and background events are chosen such that they can easily be fulfilled by the proposed ATLAS and CMS experiments. As the proposed criteria are robust and relatively simple, they are necessarily not optimised and significant improvements are possible once the real detector behaviours are known. However, the proposed analysis demonstrates the potential of a fast Higgs discovery in this mass range.

### 3 Selection Cuts

The goal of this analysis is to show that the expected large rate of the  $pp \to H \to W^+W^- \to \ell^+\nu\ell'^-\bar{\nu}$  can compensate the absence of a narrow mass peak. In order to perform a consistent analysis, the PYTHIA Monte Carlo program is used for the simulation of signal and background events. If not specified otherwise, the program is used with the default parameter setting. For all production and decay processes we have considered only the tree-level calculation as the 1-loop calculations do not exist for all relevant background processes. This allows a consistent analysis for signal and background and our results can easily be compared with previous studies using the four-charged-leptons channel. We thus do not include any K-factors. It is however worth pointing out that the 1-loop corrections to the main Higgs production process via gluon-gluon fusion are large and positive [17] whereas the corrections to the 2-to-2 and 2-to-3 background processes are expected to be smaller [18].

The first set of selection criteria listed below selects relatively central events with two isolated charged leptons (electrons or muons) with large missing energy due to the two (or more) neutrinos. These cuts are mostly comparable to [13, 14]. Starting from this initial set of cuts, one can concentrate on the differences between events originating from the Higgs production and from the so called "irreducible" background from continuum production of  $pp \to W^+W^-X$  events. Even though the criteria strongly reduce the events where the leptons originate from Z decays, they are not yet sufficient for a complete removal of this possible background. As will be shown below, this background is essentially removed by a stronger requirement, cut 9, on the opening angle  $\phi$  between the two leptons in the plane transverse to the beam.

1. The event should contain two leptons with opposite charge each with a minimal  $p_t$  of 10 GeV. At least one of the two leptons should have a  $p_t$  of more than 20 GeV. Furthermore, the two leptons should be separated in space by more than 10°.

<sup>&</sup>lt;sup>1</sup>We are grateful to L. Rurua, who reminded us of this potential background.

LHC 14 TeV		Accepted event fraction		
reaction $pp \to X$	$\sigma  imes BR^2  ext{ [pb]}$	cut 1-3	cut 4-6	cut 7
$pp \to H \to W^+W^- \ (m_H = 170 \text{ GeV})$	1.24	0.21	0.18	0.080
$pp  o W^+W^-$	7.4	0.14	0.055	0.039
$pp \to t\bar{t} \ (m_t = 175 \ {\rm GeV})$	62.0	0.17	0.070	0.001
$pp \to Wtb \ (m_t = 175 \text{ GeV})$	≈6	0.17	0.092	0.013
$pp  o ZW  o \ell^+\ell^-\ell\nu$	0.86	0.23	0.054	0.026
$pp \rightarrow ZZ \rightarrow 4$ -leptons	1.05	0.13	0.016	0.007
$pp  o Z  o  au^+ au^-$	1400	0.007	0.0004	0.00009
$pp \rightarrow Z \rightarrow e^+e^-, \mu^+\mu^-$	2800	0.22	0.0004	0.00012

Table 1: The expected signal and background event rates using the cross section estimates with the CTEQ2L structure functions and with the first set of selection criteria. In all cases only the leptonic W branching ratios are simulated ( $W \to \ell^{\pm} \nu$  with  $\ell^{\pm}$  being electrons, muons or  $\tau$ ). For the production of ZZ events, the cross section is obtained including the Z decays into charged leptons and neutrinos. For the production of WZ and for the single Z production only the Z decays to charged leptons including the subsequent  $\tau$  decays are simulated.

- 2. The pseudorapidity  $|\eta|$  of each lepton should be smaller than 2. For events which contain additional isolated photons with a minimal  $p_t$  of 20 GeV and  $|\eta|$  smaller than 2.4 the photon four momentum vector is added to the dilepton system.
- 3. In order to have isolated leptons it is required that the energy sum originating from hadrons and photons found within a cone of 20 degree half angle around the lepton direction should be smaller than 5 GeV.
- 4. The dilepton mass,  $m_{\ell\ell(\gamma)}$ , has to be smaller than 80 GeV.
- 5. The missing  $p_t$  of the event, required to balance the  $p_t$  vector sum of the two leptons,  $\ell\ell(\gamma)$ , should be larger than 20 GeV.
- 6. The two leptons should not be back to back in the plane transverse to the beam direction. The opening angle between the two leptons in this plane should be smaller than 135°. In order to remove the backgrounds from Z decays, this cut will be strengthened considerable in the following.
- 7. Events which have a jet with a  $p_t$  of more than 20 GeV and a pseudorapidity  $|\eta|$  of less than 2.4 are removed.

Dilepton events, originating from the decays of W and Z bosons are selected with criteria 1–3. Lepton pairs  $\ell\ell(\gamma)$  originating from single Z production with subsequent decays to leptons, including the leptons coming from decays of  $\tau$  leptons are mostly removed with criteria 4–7. Backgrounds from  $t\bar{t}$  and Wtb production, [19], are reduced strongly by the jet veto, criterion 7. It can be expected that even better background rejection factors can be obtained if some jet detection is possible up to larger values of  $|\eta|$ .

The estimated cross sections before and after the above criteria for different signal and background processes, including the leptonic branching ratios of the W's and Z are given in

table 1. As can be seen from table 1, the above set of selection criteria reduces background from  $pp \to ZX$  events by a factor of about  $10^4$ . For the following we concentrate on the remaining background from continuum production of  $W^+W^-$ ,  $t\bar{t}$  and Wtb events.

In order to distinguish a possible signal from the remaining background we use the following criteria:

- 8. The polar angle  $\theta_{\ell^+\ell^-}$  of the dilepton system, reconstructed from the vector sum of their measured momenta should fulfill  $|\cos \theta_{\ell^+\ell^-}| < 0.8$ .
- 9. The opening angle  $\phi$  between the two charged leptons in the plane transverse to the beam should be between  $10^{\circ}-45^{\circ}$ .
- 10. The mass, estimated for the assumed  $W^+W^-$  system should be larger than 140 GeV. The mass is estimated from the approximation that the two neutrinos compensate the  $p_t$  of the two charged leptons, e.g. assuming  $p_t(H) \approx 0$ , and that the mass of the undetected neutrinos is on average equal to the mass of the two charged leptons. The energy carried by the two neutrinos is thus approximated with  $E_{\nu\nu} = \sqrt{m_{\ell\ell}^2 + p_t^2(\ell\ell)}$ . With this approximation a broad mass distribution, with a mean value in agreement with the simulated Higgs mass and a large rms of about 55 GeV, is obtained.
- 11. The opening angle  $\theta^*$  between the lepton with the larger  $p_t$ , boosted to the dilepton rest frame and the momentum vector of the dilepton system should fulfill the condition  $0. < \cos \theta_{t+t-}^* < 0.3$ .

Condition eight exploits the smaller boost of the candidate events, originating from the gluon-gluon fusion process. A large fraction of the continuum  $W^+W^-$  background originates from valence-quark sea-antiquark scattering with a relatively large momentum imbalance, resulting in a boosted  $W^+W^-$  system, as shown in figure 1.

Criterion nine makes use of the spin correlation between the  $W^+W^-$  pair. The potential discriminating power of this correlation in the Higgs search has previously been pointed out by C. A. Nelson [16]. W pairs originating from the decay of a scalar have to have opposite spin orientation. Due the V-A structure in the W decay, the left handed  $e^-$  (right handed  $e^+$ ) is emitted along the  $W^-$  ( $W^+$ ) spin. As a result, one of the two charged leptons is emitted along the momentum direction of the two W's while the other one is emitted in the opposite direction. For the considered Higgs mass range, a small opening angle between the two charged leptons can be expected for signal events while the backgrounds will show an almost symmetric distribution. The discriminating power of this criterion is shown in figure 2. As can be seen the leptons originating from Higgs decays have a relatively small opening angle while the ones coming from continuum  $W^+W^-$  and  $t\bar{t}$  events show essentially a symmetric distribution.

The estimated invariant mass of the  $\ell^+\ell^-\nu\nu$  system, shown in figure 3, is unfortunately very broad. Nevertheless it discriminates to some extent between signal and background.

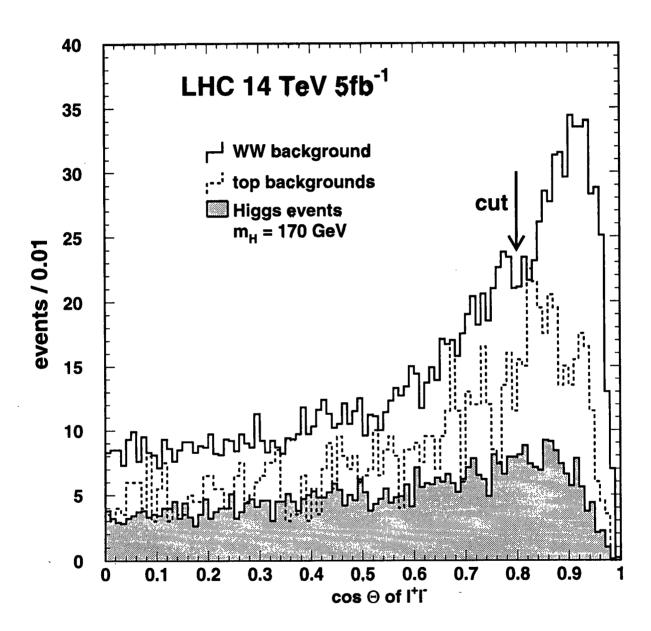


Figure 1:  $|\cos \theta|$  distribution of the dilepton system with respect to the beam direction for Higgs signal and background events.

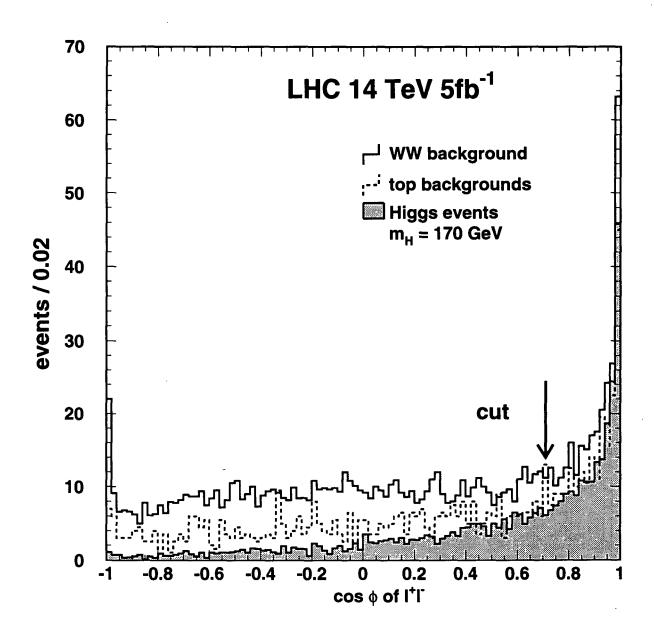


Figure 2:  $\cos \phi$  distribution of the dilepton system in the plane transverse to the beam direction for Higgs signal and background events, cut number 6 has not yet been applied.

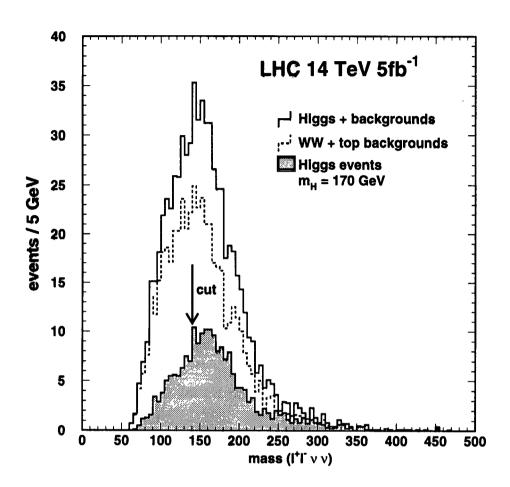


Figure 3: Estimated invariant mass of the  $\ell\ell\nu\nu$  system for Higgs signal and background events.

Finally, the two charged leptons from Higgs events show a smaller momentum spread than the ones from the background. This fact shows up nicely in figure 4, where the signal events show a peak like structure for small values of  $\cos\theta_{\ell+\ell-}^*$  while the backgrounds show a strong increase to larger values. This distribution has also some sensitivity to the Higgs mass and can therefore be used for a mass estimate.

Table 2 shows the number of accepted signal and background events for an integrated luminosity of 5 fb<sup>-1</sup> at the LHC with 14 TeV center of mass energy. Taking the signal and background event rates for the considered luminosity of 5 fb<sup>-1</sup> statistical significant signals appear already after cuts 1–7. However, as signal and background cross sections are not well known, a signal to background ratio of about 1 to  $\approx 10$  is perhaps not sufficient. As has been discussed above, with the subsequent criteria, signal to background ratios of about 1 to 1 can be obtained while keeping sizeable signal rates. Furthermore, as can be seen from figures 1–4, absolute background rates can be estimated from several distributions where clear separations between a Higgs signal and backgrounds are obtainable.

Using all criteria we obtain Higgs signals with a significance between 5-10 sigma for the

Structure Function CTEQ2L								
LHC 14 TeV		Expected event rate for 5 fb <sup>-1</sup>						
reaction $pp \to X$	$\sigma  imes Br^2  ext{ [pb]}$	cut 1-7	cut 8-9	cut 10	cut 11			
$pp \to H \ (m_H = 155 \text{GeV})$	1.09	426	168	99	49			
$pp \rightarrow H \ (m_H = 160 { m GeV})$	1.25	508	212	140	78			
$pp \rightarrow H \ (m_H = 165 \text{GeV})$	1.27	520	220	151	86			
$pp \rightarrow H \ (m_H = 170 { m GeV})$	1.24	497	201	147	74			
$pp \to H \ (m_H = 175 \text{GeV})$	1.19	462	176	129	59			
$pp \rightarrow H \ (m_H = 180 \text{GeV})$	1.11	398	151	112	47			
$pp  o W^+W^-$	7.4	1458	273	130	38			
$pp \to t\bar{t} \ (m_t = 175 { m GeV})$	62.5	441	104	72	18			
$pp \rightarrow Wtb \ (m_t = 175 \text{ GeV})$	$\approx 6$	397	110	70	24			
$pp \rightarrow ZZ, WZ$	1.9	150	31	16	5			
pp  o Z	4200	2355	49	24	$7 (\leq 13)$			
∑ all backgrounds		4781	567	312	92			
Structure Function EHLQ set 2								
$pp  o H \ (m_H = 170 \ { m GeV})$	1.7	653	263	185	92			
$pp  o W^+W^-$	5.9	1152	231	110	35			
$pp  o t ar{t} \; (m_t = 175 \; { m GeV})$	95	741	163	104	24			

Table 2: The expected event rates for signal and background for an integrated luminosity of 5 fb<sup>-1</sup> using a PYTHIA simulation and CTEQ2L. For a comparison the most important background rates are also given for the EHLQ structure functions.

considered mass range and an integrated luminosity of about 5 fb<sup>-1</sup>. This result should be compared to the significance obtained for the gold plated four charged lepton channel where about 100 fb<sup>-1</sup> are required for a 5 sigma signal.

### 4 Conclusions

We have reconsidered the signature of two leptons plus missing energy as a signal for the Higgs boson decay mode  $H \to W^+W^-$ . It is found that the Higgs detection in the previously considered difficult mass range between 155–180 GeV appears to be relatively easy for this decay signature. Using a few simple experimental criteria, clear differences between signal and backgrounds are obtained allowing a 5–10 sigma Higgs signal detection with an integrated luminosity of about 5 fb<sup>-1</sup>. We thus conclude that for the considered mass range events with two leptons plus missing energy will provide, the Higgs discovery signature at the LHC.

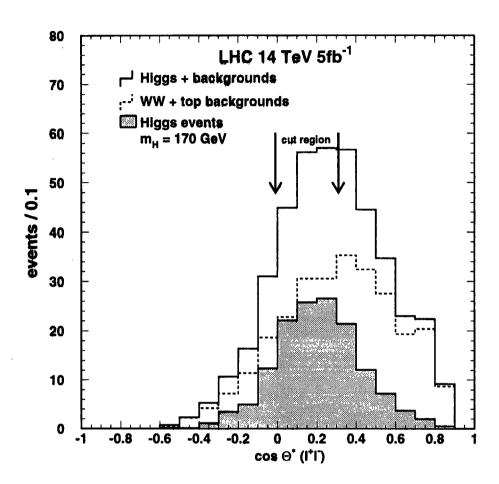


Figure 4:  $\cos \theta^*$  distribution in the dilepton rest frame for Higgs signal and background events.

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