

# Thresholds in $\alpha_s$ Evolution and the $p_T$ Dependence of Jets

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# Thresholds in $\alpha_s$ evolution and the $p_T$ dependence of jets

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#### Abstract

We point out that high-mass thresholds in the evolution of the strong-interaction coupling parameter  $\alpha_s$ , due to gluinos, squarks and possible new heavy quarks, could introduce appreciable corrections to the transverse momentum dependence of jet production at the Tevatron. If the new thresholds were near scale  $\mu=200$  GeV, then within the limits of asymptotic freedom they could introduce up to 11% increase in  $\alpha_s(\mu)$  (and hence 23% increase in jet production) at scale  $\mu=500$  GeV, compared to Standard Model extrapolations.

The CDF experiment at the Fermilab Tevatron collider has recently reported that inclusive jet production in  $p\bar{p}$  collisions appears to exceed next-to-leading order QCD expectations in the transverse momentum range  $200 < p_T(j) < 420$  GeV [1]. It has been suggested that the discrepancy might be explained by a modified gluon distribution in the nucleon [2]. However, it is also possible that some new physics may be playing a significant role. In the present note we point out that high-mass thresholds due to gluinos  $(\tilde{g})$  and squarks  $(\tilde{q})$ , plus possible new non-standard quarks (Q) and squarks  $(\tilde{Q})$ , would change the evolution of the QCD coupling parameter  $\alpha_s(\mu)$  at large values of the scale  $\mu \gtrsim m_{\tilde{g}}, m_{\tilde{q}}, m_{Q}, m_{\tilde{Q}}$ . This effect could give a significant enhancement above standard expectations, both for  $\alpha_s(\mu)$  at large  $\mu$  and hence also for the jet production cross section at large  $p_T$ , although the relation between  $p_T$  and  $\mu$  is an open question that can only be settled by higher order calculations.

The evolution equation for  $\alpha_s(\mu)$  at one loop can be written

$$\frac{d}{dt}[\alpha_s(\mu)]^{-1} = \frac{b_3}{2\pi},\tag{1}$$

with

$$b_3 = 11 - \frac{2}{3}n_f, \tag{2}$$

where  $t = \ln \mu$  and  $n_f$  is the number of quark flavors that are active, i.e. that have  $\mu > m_q$  [3]. In a supersymmetric (SUSY) model,  $b_3$  reduces by two units above the gluino threshold and by  $\frac{1}{3}$  above each successive squark threshold (assuming degenerate L- and R-chiral squarks), giving

$$b_3 = 9 - \frac{2}{3}n_f - \frac{1}{3}\tilde{n}_f,\tag{3}$$

where we assume the gluino is active and  $\tilde{n}_f$  denotes the number of active squark flavors. It is clear that as the scale  $\mu$  increases, successively more thresholds are crossed and the rate of evolution of  $[\alpha_s(\mu)]^{-1}$  decreases. Accordingly, the rate of fall of  $\alpha_s(\mu)$  as  $\mu$  increases (asymptotic freedom) is reduced with each successive threshold. Further new physics, for example new iso-singlet quarks  $Q_i$  and their SUSY partners  $\tilde{Q}_i$  (that appear naturally in the [27]-plet of  $E_6$  symmetry [4, 5]) would reduce  $b_3$  even more [6]; each counts the same as a conventional quark or squark in Eq.(3). Alternatively, a fourth generation would add two quark plus two squark flavors[7] (implications of  $\alpha_s$  evolution for high- $p_T$  jets are mentioned in Ref.[8]). With three new quarks plus squarks the value  $b_3 = 0$  is reached and we can go no further without breaking asymptotic freedom (AF). Although AF is not

necessarily an inviolable principle, it is an attractive feature that protects perturbative calculations at high energy; we therefore limit our present illustrations to cases up to the AF limit.

The solid curve in Fig.1 shows the one-loop evolution of  $\alpha_s(\mu)$  versus  $\mu$  for the standard model (SM) colored-particle content. The dotted curve shows the change to the minimum supersymmetric extension (MSSM), assuming for simplicity a common squark/gluino threshold at  $\mu = m_{\tilde{q}} = m_{\tilde{g}} = 200$  GeV (which is just below the present Tevatron bound[9]). The dot-dashed curve shows the effect of adding three singlet quarks with the same threshold; the case of one or two singlet quarks can be obtained by interpolation between dotted and dot-dashed curves. Finally the horizontal dashed curve shows that adding three singlet squarks too, with the same threshold, brings us to the AF limit. The dashed curve lies above the solid SM curve by a factor 1.11 at scale  $\mu = 500$  GeV.

The inclusive jet production cross section  $\sigma(p\bar{p}\to jX)$  at the Tevatron is based on  $2\to 2$  QCD parton subprocesses that are proportional to  $[\alpha_s(\mu)]^2$ . A common choice for the scale  $\mu$  here is  $\mu=p_T(j)/2$ , in terms of the jet transverse momentum  $p_T$ ; in this case the new threshold effects of Fig.1 would only be felt for  $p_T>400$  GeV, i.e. mostly beyond the range of the reported Tevatron data[1]. However, for the choice  $\mu=p_T(j)$  instead, the effects of Fig.1 would give an enhancement for  $p_T>200$  GeV; at  $p_T=500$  GeV this enhancement ranges between 12% (for the MSSM case) and 23% (for the AF limit case). The relationship between  $\mu$  and  $p_T$  could be determined in principle by higher-order calculations of jet production, including the physics beyond the Standard Model in the loops, but for the present it remains an open question.

We conclude that new thresholds in the evolution of  $\alpha_s$  are capable of providing substantial increases in the jet hadroproduction cross section at large  $p_T(j)$ , and may be significant contributors to the reported effect.

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# Figure captions

Fig.1. The one-loop evolution of  $\alpha_s(\mu)$  versus  $\mu$  is compared in various scenarios, normalized to  $\alpha_s(M_Z)=0.12$ . The solid curve is the SM prediction, with  $m_t=175$  GeV. The dotted curve is the MSSM prediction, with a common squark/gluino threshold at  $\mu=200$  GeV. The dot-dashed curve shows the effect of three singlet quarks with common mass  $m_Q=200$  GeV. The dashed curve, which reached the AF limit, shows the further effect of three singlet squarks if  $m_{\tilde{Q}}=200$  GeV.



