

Science and Engineering Research Council

Rutherford Appleton Laboratory

Chilton DIDCOT Oxon OX11 0QX

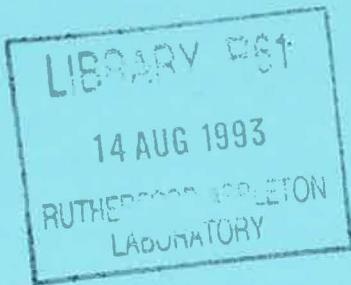
RAL-93-061

RAL-93-061

RAL 93061
COPY 2 1261
ACC N 220066

GKS-9x: A Specification of the Framework

L B Damnjanovic and D A Duce



August 1993

Science and Engineering Research Council

"The Science and Engineering Research Council does not accept any responsibility for loss or damage arising from the use of information contained in any of its reports or in any communication about its tests or investigations"

GKS-9x: A Specification of the Framework

L.B. Damnjanovic and D.A. Duce

Informatics Department, Rutherford Appleton Laboratory, Chilton, Didcot, Oxon OX11 0QX, UK

1. Introduction

The Graphical Kernel System, GKS, was published as an International Standard in 1985,⁷ and is now being revised.^{1,4} Prior to exploring approaches to implementing some of the new functionality, the authors prepared a formal description of the key parts of the framework of GKS-9x which were relevant to the implementation issues which were later studied. The implementation studies are reported in the papers by Damnjanovic, Duce and Robinson.^{2,3}

The formal description used the OBJ notation and follows the approach described in Duce and Damnjanovic.⁵ The content proposed for the revised GKS, GKS-9x, has changed since the latter paper was written, but the specification follows very similar lines.

In order that this paper can be read independently from the implementation studies paper² the next section repeats much of the description of the current draft of GKS-9x contained in that paper.

2. An Overview of GKS-9x

2.1. The NDC Picture

In GKS:1985, graphical output primitives are defined by the application in a world coordinate system, are transformed to Normalized Device Coordinates (NDC) by a normalization transformation and are then passed to workstations for display. Each workstation then applies its own workstation transformation which maps a region of NDC space onto a specified region of the workstation's display space. The normalization transformation can be thought of as creating a scene in NDC space from components defined in different world coordinate systems and a workstation can be thought of as a camera viewing the scene.

The model as presented above is not actually present in GKS:1985 in such a pure form and this has led to a number of difficulties with the design of the first generation graphics standards, in particular in defining the relationship between GKS:1985 and the Computer Graphics Metafile (CGM).⁴

The first major new concept to be introduced in GKS-9x was the idea of an NDC picture, which is manipulated in well-defined ways and whose contents are always well-defined. The NDC picture is organized as a sequence of output primitives.

The overall architecture of GKS-9x is summarized in figure 1.

2.2. Namesets and Selection Criteria

The Disley workshop report recommendations listed in section 1 referred to the need for more generality in naming primitives based on the nameset concept of PHIGS.⁸ In PHIGS, a set of names (normally represented in language bindings by an array or list of integers) may be associated with an output primitive. This nameset attribute is used to control whether the primitive is visible, highlighted or detectable by a particular pick device on a particular workstation. Control is exercised by filters. A filter consists of two sets of names, an inclusion set and an exclusion set. A primitive has a particular property such as highlighting if its nameset attribute has at least one name in common with the inclusion set of the filter and no names in common with its exclusion set.

In GKS-9x, the filters have been replaced by application-specifiable selection criteria. A primitive is selected for some purpose if its nameset attribute satisfies the corresponding selection criterion. Selection

criteria are constructed from set-theoretic comparison operators (equality with a specified set of names, subset and superset of specified sets of names) and the logical operators (and, or, not). The comparison operators are:

contains(<i>ns</i>)	$ns \subseteq pns$
isin(<i>ns</i>)	$pns \subseteq ns$
equals(<i>ns</i>)	$ns = pns$
SELECTALL	True (for any nameset)
REJECTALL	False (for any nameset)

In the table above, *pns* denotes the nameset of the primitive to which the criterion is being applied and *ns* is a nameset supplied as parameter to the operator.

As an example, the criterion:

contains({SWAN, LAKE})

selects all primitives tagged with 'SWAN' and 'LAKE', while:

not contains({SWAN, LAKE})

would select all other primitives. Selection criteria are explained in more detail in a later section.

The main difference between selection criteria and PHIGS filters is that for filters the function applied to namesets is fixed, whereas for selection criteria the function is specified by the application. The range of uses to which namesets and selection criteria are put is much broader than the uses of namesets and filters in PHIGS, as will become evident later in this section.

2.3. Picture Part Store

To support the composition of NDC pictures, a separate picture part store has been provided. A picture part is a named sequence of output primitives. Picture parts can be copied from the picture part store to the NDC picture and a subsequence of primitives in the NDC picture which satisfy a specified selection criterion, can be copied into the picture part store.

The function to copy picture parts into the NDC picture also uses a selection criterion to select a subsequence of the primitives in the picture part for the copy operation. In addition, a specified set of names can be added to the nameset attribute of each new primitive created in the NDC picture. This enables primitives created from different copy operations on the same picture part to be distinguished.

It is envisaged that the picture part store will take over the functions of the old GKS segment store while producing a much richer storage facility.

2.4. Transformations

All primitives in GKS-9x have two transformation matrices associated with them, the global transformation and the local transformation. These attributes have been introduced in order to provide a flexible mechanism for constructing NDC pictures from picture parts. The local transformation matrix enables primitives to be composed to construct objects, or subparts of pictures. If the global transformation attributes of all the primitives making up an object are set to the same value, the effect is to control the overall positioning of the object in the NDC picture. Thus the local transformation is used to construct objects and the global transformation to control the positioning of an instance of an object in the NDC picture. Both local and global transformations can be changed when picture parts are copied into the NDC picture. In consequence, some of the modelling capabilities of PHIGS are available in GKS-9x.

2.5. Modification of the NDC Picture

The attributes of primitives in the NDC picture can be edited. The functionality provided is to set a specified attribute for every primitive in the NDC picture satisfying a specified selection criterion, to a new value. In addition, functions are provided to add or remove specified sets of names from the nameset attributes of a selected sequence of primitives in the NDC picture. These additional functions are often a more convenient way of manipulating nameset attributes than the editing function which just enables a nameset

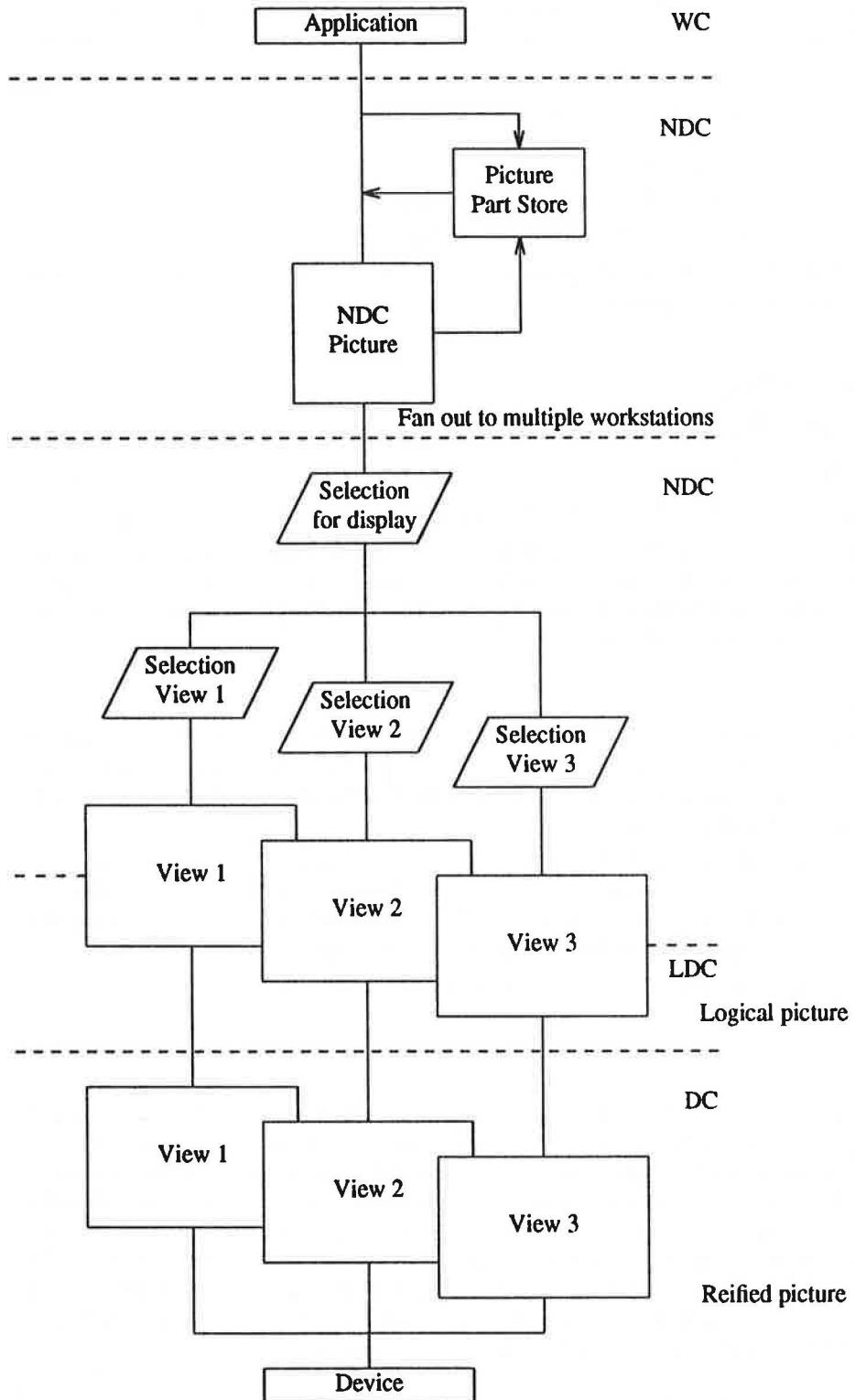


Figure 1: Architecture of GKS-9x

attribute to be replaced by a new value.

Primitives may be deleted from the NDC picture and again a selection criterion is used to specify which primitives the operation is to apply to.

As stated earlier, the NDC picture is a sequence of output primitives. This means that there is a well-defined order to the primitives in the NDC picture and this order is preserved by all the operations on the NDC picture. This order is also respected when the NDC picture is displayed on a workstation. It may sometimes be necessary to change the order of the primitives in the NDC picture and to do this, a function REORDER NDC PICTURE, is provided. This function moves the subsequence of primitives which satisfy a selection criterion to either the start or the end of the NDC picture sequence.

2.6. Display

The mechanism in GKS-9x for displaying the NDC picture on workstations is also more general than the mechanism in GKS:1985. The key idea is that each open workstation acts as a camera, viewing the NDC picture. As the NDC picture is changed, the picture displayed on the workstation is updated accordingly. The NDC picture is assumed to be always up-to-date. The function SET NDC VISUAL EFFECTS allows the continual refreshing of the workstation display to be suspended and resumed. Using the camera analogy, this is equivalent to closing and opening the shutter of the camera.

A selection criterion associated with each open workstation controls which primitives in the NDC picture are eligible for display on that workstation.

2.7. Multiple Views

In GKS:1985, the workstation transformation maps the NDC picture directly into device coordinates (DC), so that only a single view of the NDC picture is displayed on each workstation. GKS-3D and PHIGS introduced a viewing transformation applied before the workstation transformation. The motivation for the viewing transformation in these systems was obviously to perform 3D viewing operations. Multiple views could be defined on each workstation and a view index attribute associated with each primitive is used to select the particular view transformation to be applied.

In fact the idea of viewing is just as relevant in 2D as in 3D, and so GKS-9x contains a view transformation between the NDC picture and the workstation transformation. The GKS-9x viewing mechanism is a generalization of the GKS-3D and PHIGS mechanisms. In those systems a single primitive can only be subjected to a single viewing operation. In GKS-9x, multiple view transformations can be defined, and a primitive can be displayed in any of the defined views. Selection criteria associated with the views determine which primitives appear in which views of the NDC picture. One of the extensions made by some PHIGS implementations has been to add similar facilities.

The NDC picture is transformed into a logical picture on the workstation, partitioned into views by the view transformations. The logical picture is defined in Logical Device Coordinates (LDC). Output primitives in the logical picture have logical attributes and NDC attributes bound to them. The attribute binding mechanism is exactly the same as GKS:1985, though the description has been changed somewhat to provide a more comprehensible description in the GKS-9x framework. The logical picture is then transformed into the reified picture which is realized on the workstation's display space.

2.8. Interfaces

GKS-9x has been developed in step with the Computer Graphics Reference Model (CGRM).⁹ The GKS-9x framework maps readily into the framework provided by the CGRM. Some formal description work has been carried out to verify this claim.⁶

GKS-9x has also introduced the concept of a backdrop. Primitives may be routed to the backdrop, in which case they do not form part of the NDC, logical or reified pictures. This can be useful for applications which generate large volumes of graphical data which do not require any manipulation.

2.9. New Primitives

GKS-9x has introduced many other improvements, for example additional types of output primitives have been included to generate non-uniform B-spline curves, conic sections, conic sectors and conic segments. However, the implementation work which is the subject of this paper did not address these areas of GKS-9x and so they are not described any further here.

2.10. Operations Modelled

The GKS-9x operations modelled in the specification are:

```
OPEN GKS
CREATE OUTPUT PRIMITIVE
SET PRIMITIVE ATTRIBUTE
ADD SET OF NAMES TO NAMESET
REMOVE SET OF NAMES FROM NAMESET
SET WINDOW AND VIEWPORT
SET NORMALIZATION TRANSFORMATION NUMBER
DELETE PRIMITIVES
REMOVE SET OF NAMES FROM NDC PICTURE
ADD SET OF NAMES TO NDC PICTURE
SET NDC PICTURE PRIMITIVE ATTRIBUTE
REORDER NDC PICTURE
BEGIN PICTURE PART
BEGIN PICTURE PART AGAIN
END PICTURE PART
APPEND PICTURE PART
RENAME PICTURE PART
DELETE PICTURE PART
COPY PICTURE PART FROM PICTURE PART STORE
COPY NDC PICTURE TO PICTURE PART STORE
OPEN WORKSTATION
CLOSE WORKSTATION
SET REPRESENTATION
SET VIEW SELECTION CRITERION
SET VIEW
SET NDC VISUAL EFFECTS
SET WORKSTATION WINDOW AND VIEWPORT
SET WORKSTATION SELECTION CRITERION
```

3. The GKS-9x Specification

3.1. Structure

The specification consists of a number of OBJ modules, described below.

3.2. INTEGER

Coordinate systems in GKS are based on real numbers. The OBJ interpreter used in this work only supported natural numbers. For the purposes of this specification, coordinates were expressed as integers and a mapping of integers onto natural numbers was provided.

```
obj INTEGER
sorts int
ops _+_ : int int → int (ASSOC COMM )
      _-_ : int int → int
      *_ : int int → int (ASSOC COMM )
      _div_ : int int → int
      ps_ : nat → int
      ng_ : nat → int
vars i,j : int
      n,m : nat
eqns (ps n + ps m = ps (n+m))
      (ng n + ps m = ps (m-n) IF (m>n))
      (ng n + ps m = ng (n-m) IF (n>m))
      (ng n + ng m = ng (n+m))
      (ng n + ps m = ps (m-m) IF (n==m))
```

($ps\ n - ps\ m = ps\ (n-m)$ IF ($n > m$))
($ps\ n - ps\ m = ng\ (m-n)$ IF ($m > n$))
($ps\ n - ps\ m = ps\ (n-m)$ IF ($n == m$))
($ng\ n - ng\ m = ng\ (n+m)$)
($ps\ n - ng\ m = ps\ (n+m)$)
($ng\ n - ps\ m = ng\ (n+m)$)

($ng\ n * ps\ m = ng\ (m*n)$)
($ng\ n * ng\ m = ps\ (m*n)$)
($ps\ n * ps\ m = ps\ (n*m)$)

($ps\ n \text{ div } ps\ m = ps\ (n \text{ div } m)$)
($ps\ n \text{ div } ng\ m = ng\ (n \text{ div } m)$)
($ng\ n \text{ div } ps\ m = ng\ (n \text{ div } m)$)
($ng\ n \text{ div } ng\ m = ps\ (n \text{ div } m)$)

jbo

3.3. NAMES

This object defines the basic sorts for names, picture part names, workstation identifiers and normalization transformation numbers. For illustration, limited numbers of constants of each sort are defined.

obj NAMES
sorts *Name* *PicPartName* *WsId* *NormTran*
ops *WPT1:* → *Name*
WPT2: → *Name*
WPT3: → *Name*
NAM,BIG,BEN: → *Name*
IME,RED,BALL: → *Name*
TRIANGLE,SMALL: → *Name*
POINT,A,B,LINE: → *Name*
BLUE,GREEN,HAT: → *Name*
N4: → *Name*
N5: → *Name*
N6: → *Name*
N7: → *Name*
NONAMEPN: → *PicPartName*
P1: → *PicPartName*
P2: → *PicPartName*
P3: → *PicPartName*
P4: → *PicPartName*
OPENPP: → *PicPartName*
W1: → *WsId*
W2: → *WsId*
W3: → *WsId*
W4: → *WsId*
pptoname: *PicPartName* → *Name*
wsidtoname: *WsId* → *Name*
NTN0: → *NormTran*
NTN1: → *NormTran*
NTN2: → *NormTran*

jbo

3.4. NAMESETS

This object defines the basic operations on namesets (sets of *Name*s), including operations to add a name to a nameset (*addname*), remove a name from a nameset (*removessn*), remove a set of names from a nameset (*subtractset*) and test for membership of a nameset (*member*).

```

obj NAMESETS /NAMES
sorts NameSet
ops emptyNS: → NameSet
    _U : NameSet NameSet → NameSet (ASSOC COMM ID:emptyNS)
    addname: Name NameSet → NameSet
    mkSet: Name → NameSet
    renamessn: Name Name NameSet → NameSet
    subtractset: NameSet NameSet → NameSet
    removessn: Name NameSet → NameSet
    member: Name NameSet → BOOL
vars ns,ns1,ns2:NameSet
    on,nn,n,n1,m:Name
eqns ((ns) U (ns)) = ns
    (addname(n,ns) = (mkSet(n)) U (ns))
    (renamessn(on,nn,emptyNS) = emptyNS)
    (renamessn(on,nn,(ns1) U (ns2)) = (renamessn(on,nn,ns1)) U (renamessn(on,nn,ns2)))
    (renamessn(on,nn,mkSet(n)) = mkSet(n) IF not (on == n))
    (renamessn(on,nn,mkSet(on)) = mkSet(nn))

    (subtractset(ns,(ns1) U (ns2)) = (subtractset(ns,ns1)) U (subtractset(ns,ns2)))
    (subtractset((ns1) U (ns2),ns) = subtractset(ns2,subtractset(ns1,ns)))
    (subtractset(ns,emptyNS) = emptyNS)
    (subtractset(ns,ns) = emptyNS)
    (subtractset(emptyNS,ns) = ns)
    (subtractset(mkSet(n),mkSet(n1)) = mkSet(n1) IF not (n == n1))

    (removessn(n,(ns1) U (ns2)) = (removessn(n,ns1)) U (removessn(n,ns2)))
    (removessn(n,emptyNS) = emptyNS)
    (removessn(n,mkSet(n)) = emptyNS)
    (removessn(n,mkSet(n1)) = mkSet(n1) IF not (n == n1))

    (member(n,emptyNS) = F)
    (member(n,mkSet(m)) = (n==m))
    (member(m, (ns1) U (ns2)) = (member(m,ns1)) or (member(m,ns2)))

```

jbo

3.5. ATTRIBUTES

For illustration, a limited number of constants of each sort of attribute values are defined. The operation *selectlogattr* selects the value of a logical attribute from individually specified values or from a bundle, depending on the value of the corresponding attribute source flag.

```

obj MATRIX23/ INTEGER
sorts Matrix23
ops mktransfcor: int int int int int int → Matrix23
    mult: Matrix23 Matrix23 → Matrix23
vars a,b,c,d,e,f,g,h,z,l,m,n:int
eqns (mult(mktransfcor(a,b,c,d,e,f), mktransfcor(g,h,z,l,m,n))
    = mktransfcor((a*g)+(d*h),(b*g)+(e*h),(c*g)+(f*h)+z,(a*l)+(d*m),(b*l)+(e*m),(c*l)+(f*m)+n))

```

jbo

```

obj ATTRIBUTES /NAMESETS MATRIX23
sorts Identification Source Logical NDCattr asfs ASF PlInd
    Linetype Linewidth Highl Det PlBun TransMode
ops identifa: NameSet → Identification
    asfsa: ASF ASF → asfs
    sourcea: asfs PlInd → Source
    logicala: Linetype Linewidth → Logical
    ndca: Matrix23 Matrix23 → NDCattr
    REPLACE, PRE, POST: → TransMode
    modifyndca: Matrix23 TransMode Matrix23 TransMode NDCattr → NDCattr
    mkBundle: Linetype Linewidth → PlBun
    selectlogattr: asfs Logical PlBun → Logical
    LOCAL, GLOBAL: → Matrix23
    INDIVIDUAL, BUNDLED: → ASF
    PLI0, PLI1, PLI2: → PlInd
    SOLID, DASHED, DOTTED: → Linetype
    THIN, THICK, MEDIUM: → Linewidth
    NORMAL, HIGHLIGHTED: → Highl
    DETECTABLE, UNDETECTABLE: → Det
vars lt,lt1: Linetype
    lw,lw1: Linewidth
    global,global1,local,local1: Matrix23
    trmode, trmodel: TransMode
eqns (modifyndca(global,REPLACE,local,REPLACE,ndca(local1,global1)) = ndca(local,global))
    (modifyndca(global,REPLACE,local,PRE,ndca(local1,global1))
     = ndca(mult(local1,local), global))
    (modifyndca(global,REPLACE,local,POST,ndca(local1,global1))
     = ndca(mult(local,local1), global))
    (modifyndca(global,PRE,local,REPLACE,ndca(local1,global1))
     = ndca(local,mult(global1, global)))
    (modifyndca(global,POST,local,REPLACE,ndca(local1,global1))
     = ndca(local,mult(global,global1)))
    (modifyndca(global,PRE,local,PRE,ndca(local1,global1))
     = ndca(mult(local1,local), mult(global1, global)))
    (modifyndca(global,POST,local,POST,ndca(local1,global1))
     = ndca(mult(local,local1), mult(global,global1)))

    (selectlogattr(asfsa(BUNDLED,BUNDLED),logicala(lt,lw), mkBundle(lt1,lw1))
     = logicala(lt1,lw1))
    (selectlogattr(asfsa(BUNDLED,INDIVIDUAL),logicala(lt,lw), mkBundle(lt1,lw1))
     = logicala(lt1,lw))
    (selectlogattr(asfsa(INDIVIDUAL,BUNDLED),logicala(lt,lw), mkBundle(lt1,lw1))
     = logicala(lt,lw1))
    (selectlogattr(asfsa(INDIVIDUAL,INDIVIDUAL),logicala(lt,lw), mkBundle(lt1,lw1))
     = logicala(lt,lw))

jbo

```

3.6. SELECTION

This object defines selection criteria and an operation *satisfy* which delivers true (*T*) if a nameset satisfies a given selection criterion and false (*F*) if it does not.

```

obj SELECTION / NAMESETS ATTRIBUTES
sorts SelectCrit SelectDisp SelectHighl SelectDet
ops SELECTALL,REJECTALL: → SelectCrit

```

```

DISPLAY: → SelectDisp
HIGHLIGHTING: → SelectHighl
DETECTABILITY: → SelectDet
contains: NameSet → SelectCrit
isin: NameSet → SelectCrit
sequals : NameSet → SelectCrit
sand: SelectCrit SelectCrit → SelectCrit
sor: SelectCrit SelectCrit → SelectCrit
snot: SelectCrit → SelectCrit

satisfy: NameSet SelectCrit → BOOL

highlt: NameSet SelectCrit → Highl
dect: NameSet SelectCrit → Det
vars ns,ns1,ns2:NameSet
n:Name
s,s1,s2:SelectCrit
h:Highl
d:Det
Selcrit,sv,sh,sd:SelectCrit
wsid:WsId
eqns (satisfy(ns,sand(s1,s2)) = (satisfy(ns,s1)) and (satisfy(ns,s2)))
(satisfy(ns, sor(s1,s2)) = (satisfy(ns,s1)) or (satisfy(ns,s2)))
(satisfy(ns, snot(s)) = not(satisfy(ns,s)))
(satisfy(ns,contains(mkSet(n))) = member(n,ns))
(satisfy(ns,contains(emptyNS)) = T)
(satisfy(ns,contains((ns1)U(ns2))) = (satisfy(ns,contains(ns1))) and (satisfy(ns,contains(ns2))))
(satisfy(emptyNS,isin(ns)) = T)
(satisfy(mkSet(n),isin(ns)) = member(n,ns))
(satisfy((ns1) U (ns2),isin(ns)) = satisfy(ns1,isin(ns)) and satisfy(ns2,isin(ns)))
(satisfy(ns,sequals(ns1)) = (ns==ns1))
(satisfy(ns,SELECTALL) = T)
(satisfy(ns,REJECTALL) = F)

(highlt(ns,sh) = HIGHLIGHTED IF (satisfy(ns,sh)==T))
(highlt(ns,sh) = NORMAL IF not(satisfy(ns,sh)==T))

(dect(ns,sd) = DETECTABLE IF (satisfy(ns,sd)==T))
(dect(ns,sd) = UNDETECTABLE IF not(satisfy(ns,sd)==T))
jbo

```

3.7. TABLE

This object defines a general table sort which is used later to define bundle and other tables.

```

obj TABLE
sorts tb index telem
ops emptyTb: → tb
      _U_: tb tb → tb (ASSOC COMM ID:emptyTb)
      %_ : index telem → tb
      \_ : tb index → tb
      +_ : tb tb → tb
      [ ]: tb index → telem
vars t1,t2: tb
      i,j: index

```

```

el: telem
eqns ((t1)U(t1) = t1)
      ((i % el)(i) = emptyTb)
      ((emptyTb)\(i) = emptyTb)
      ((j % el)(i) = (j % el) IF not (i==j))
      (((t1) U (t2)))\((i) = ((t1)\(i)) U ((t2)\(i)))
      ((t1) + (i % el) = ((t1)\(i)) U ((i % el)))
      (((t1) U (i % el))[ i] = el)
      (((t1) U (i % el))[ j] = t1[ j] IF not (i==j))

```

jbo

3.8. NDCPOINT, NDCPOINTS, LISTOFNDCPOINTS

These objects define points in WC and NDC coordinates, list of such points and an operation to transform lists of points from WC to NDC.

```

obj NDCPOINT /MATRIX23 INTEGER
sorts WCPoint NDCPoint
ops mkWCPoint: int int → WCPoint
mkNDCPoint: int int → NDCPoint
transf: WCPoint Matrix23 → NDCPoint
transfNDC: NDCPoint Matrix23 → NDCPoint
X,Y: → int
vars x,y,a,b,c,d,e,f: int
eqns (transf(mkWCPoint(x,y),mktransfcor(a,b,c,d,e,f))
      = mkNDCPoint((x*a)+(y*b)+c, (x*d)+(y*e)+f))
      (transfNDC(mkNDCPoint(x,y),mktransfcor(a,b,c,d,e,f))
      = mkNDCPoint((x*a)+(y*b)+c, (x*d)+(y*e)+f))

```

jbo

```

obj NDCPOINTS /NDCPOINT
sorts WCPoints NDCPoints
ops emptyWCPoints: → WCPoints
addWCpoint: WCPoint WCPoints → WCPoints
emptyNDCPoints: → NDCPoints
addNDCpoint: NDCPoint NDCPoints → NDCPoints
transfPoints: WCPoints Matrix23 → NDCPoints
transfNDCPoints: NDCPoints Matrix23 → NDCPoints
vars pn: WCPoint
ndcpoint: NDCPoint
ndcpoints: NDCPoints
pnts: WCPoints
mat: Matrix23
eqns (transfPoints(emptyWCPoints, mat) = emptyNDCPoints)
      (transfPoints(addWCpoint(pn,pnts), mat) = addNDCpoint(transf(pn,mat), transfPoints(pnts,mat)))
      (transfNDCPoints(emptyNDCPoints, mat) = emptyNDCPoints)
      (transfNDCPoints(addNDCpoint(ndcpoint, ndcpoints), mat)
      = addNDCpoint(transfNDC(ndcpoint,mat), transfNDCPoints(ndcpoints,mat)))

```

jbo

```

obj LISTOFNDCPOINTS /NDCPOINTS
sorts ListofWCP ListofNDCP
ops emptyLofWCP: → ListofWCP
addWCpoints: WCPoints ListofWCP → ListofWCP
emptyLofNDCP: → ListofNDCP

```

```

addNDCpoints: NDCPoints ListofNDCP → ListofNDCP
transfLofPoints: ListofWCP Matrix23 → ListofNDCP
transfLofNDCPoints: ListofNDCP Matrix23 → ListofNDCP
LWCP1,LWCP2,LWCP3,LWCP4,LWCP5: → ListofWCP
vars pnts: WCPoints
      lopnts: ListofWCP
      ndcpoints: NDCPoints
      lndcpoints: ListofNDCP
      mat: Matrix23
eqns (transfLofPoints(emptyLofWCP, mat) = emptyLofNDCP)
      (transfLofPoints(addWCpoints(pnts, lopnts), mat)
       = addNDCpoints(transfPoints(pnts, mat), transfLofPoints(lopnts, mat)))
      (transfLofNDCPoints(emptyLofNDCP, mat) = emptyLofNDCP)
      (transfLofNDCPoints(addNDCpoints(ndcpoints, lndcpoints), mat)
       = addNDCpoints(transfNDCPoints(ndcpoints, mat), transfLofNDCPoints(lndcpoints, mat)))
jbo

```

3.9. LISTOFNT

This object defines a list of normalization transformations. This is used later as a component of the GKS-9x state list.

```

image
      (TABLE => LISTOFNT) / NAMES MATRIX23
sorts (tb => ListofNT)
      (telem => Matrix23)
      (index => NormTran)
ops (emptyTb: → tb => emptyLNT)
endim

```

3.10. SETOFPOLYLINE

This object defines the SET OF POLYLINE function. This is the only primitive considered in this specification. It is represented by the list of points in NDC which define the geometry of the primitive and the identification, source and logical attributes associated with the primitive.

```

obj SETOFPOLYLINE /ATTRIBUTES LISTOFNDCPOINTS
sorts SetofPolyline
ops mkSetofPolyline: ListofNDCP Identification NDCattr Source Logical → SetofPolyline
jbo

```

3.11. PICTUREPART and PICTUREPARTSTORE

These objects define picture parts (a list of primitives) and picture part store (a set of named picture parts). Operations on picture part store are defined. These correspond closely to the GKS-9x functions which manipulate the picture part store.

```

obj PICTUREPART / SETOFPOLYLINE
sorts PicturePart
ops emptyPP: → PicturePart
      addPP: SetofPolyline PicturePart → PicturePart
      appendPP: PicturePart PicturePart → PicturePart
      addnames: NameSet PicturePart → PicturePart
      addattr: NameSet Matrix23 TransMode Matrix23 TransMode PicturePart → PicturePart
vars pp,ppl: PicturePart
      p: SetofPolyline
      ns,ns1: NameSet

```

```

lndcp: ListofNDCP
sa: Source
la: Logical
ndc: NDCattr
local, global: Matrix23
trmode, trmodel: TransMode
eqns (appendPP(emptyPP,pp) = pp )
      (appendPP(addPP(p,pp),pp1) = addPP(p,appendPP(pp,pp1)))
      (addnames(ns,emptyPP) = emptyPP)
      (addnames(ns,addPP(mkSetofPolyline(lndcp,identifa(ns1),ndc,sa,la),pp))
      = addPP(mkSetofPolyline(lndcp,identifa((ns)U(ns1)), ndc, sa, la),
              addnames(ns,pp)))
      (addattr(ns,global,trmode,local,trmodel,emptyPP) = emptyPP)
      (addattr(ns,global,trmode,local,trmodel,addPP(mkSetofPolyline(
              lndcp,identifa(ns1),ndc,sa,la),pp))
      = addPP(mkSetofPolyline(lndcp,identifa((ns)U(ns1)),
              modifyndca(global,trmode,local,trmodel,ndc), sa,la), addnames(ns,pp)))
jbo

obj PICTUREPARTSTORE / PICTUREPART
sorts PPS
ops emptyPPS: → PPS
mkPPS: PicPartName PicturePart → PPS
_U_: PPS PPS → PPS (ASSOC COMM ID:emptyPPS)
beginpicturepart: PicPartName PPS → PPS
deletepicturepart: PicPartName PPS → PPS
renamepicturepart: PicPartName PicPartName PPS → PPS
appendpicturepart: PicPartName PicPartName Matrix23 TransMode Matrix23 TransMode
NameSet PPS → PPS
getpicturepart: PicPartName PPS → PicturePart
addtoPP: PicPartName SetofPolyline PPS → PPS
PPisinPPS: PicPartName PPS → BOOL
vars pps,ppsl,pps2: PPS
pp,pp1,pp2: PicturePart
pn,pn1,pn2: PicPartName
p: SetofPolyline
local, global: Matrix23
trmode,trmodel: TransMode
ns:NameSet
eqns ((pps) U (pps) = pps)
      (mkPPS(pn,emptyPP) = emptyPPS)
      (beginpicturepart(pn,pps) = (mkPPS(pn,emptyPP)) U (pps))

      (deletepicturepart(pn,emptyPPS) = emptyPPS)
      (deletepicturepart(pn,(ppsl) U (pps2)) = (deletepicturepart(pn,ppsl)) U (deletepicturepart(pn,pps2)))
      (deletepicturepart(pn,mkPPS(pn,pp)) = emptyPPS)
      (deletepicturepart(pn,mkPPS(pn1,pp)) = mkPPS(pn1,pp) IF not(pn==pn1))

      (renamepicturepart(pn,pn1,emptyPPS) = emptyPPS)
      (renamepicturepart(pn,pn1,mkPPS(pn,pp)) = mkPPS(pn1,pp))
      (renamepicturepart(pn,pn1,(ppsl) U (pps2))
      = (renamepicturepart(pn,pn1,ppsl)) U (renamepicturepart(pn,pn1,pps2)))
      (renamepicturepart(pn,pn1,(mkPPS(pn,pp))) = mkPPS(pn1,pp))
      (renamepicturepart(pn,pn1,(mkPPS(pn2,pp))) = mkPPS(pn2,pp) IF not(pn==pn2))

```

```

(appendpicturepart(pn,pn1,global,trmode,local,trmodel,ns,pps)
= (mkPPS(pn1,appendPP(addattr(ns,global,trmode,local,trmodel, getpicturepart(pn,pps)),getpicturepart(pn1,pps)))) U
    (deletepicturepart(pn1,pps)))

(getpicturepart(pn,emptyPPS) = emptyPP)
(getpicturepart(pn,(mkPPS(pn,pp))U(pps)) = pp )
(getpicturepart(pn,(mkPPS(pn1,pp)) U (pps)) = getpicturepart(pn,pps) IF not (pn==pn1))

(PPisinPPS(pn,emptyPPS) = F)
(PPisinPPS(pn, (pps1) U (pps2)) = PPisinPPS(pn,pps1) or PPisinPPS(pn,pps2))
(PPisinPPS(pn1, mkPPS(pn,pp)) = (pn1==pn))

(addtoPP(pn,p,emptyPPS) = emptyPPS)
(addtoPP(pn,p,mkPPS(pn,pp)) = mkPPS(pn,addPP(p,pp)))
(addtoPP(pn,p,mkPPS(pn1,pp)) = mkPPS(pn1,pp) IF not(pn==pn1))
(addtoPP(pn,p,(pps1) U (pps2)) = (addtoPP(pn,p,pps1)) U (addtoPP(pn,p,pps2)))

```

jbo

3.12. NDCPICTURE

This object models the NDC picture and the operations on the NDC picture which modify the values of identification and logical attributes associated with primitives in the NDC picture.

```

obj NDCPICTURE / PICTUREPART SELECTION
sorts NDCPicture Position
ops emptyNDCP: → NDCPicture
    FRONT, BACK: → Position
    addNDCP: SetofPolyline NDCPicture → NDCPicture
    appendNDCP: NDCPicture NDCPicture → NDCPicture
    setattrNDCP: SelectCrit PlInd NDCPicture → NDCPicture
    setattrNDCP: SelectCrit asfs NDCPicture → NDCPicture
    setattrNDCP: SelectCrit Linetype NDCPicture → NDCPicture
    setattrNDCP: SelectCrit Linewidth NDCPicture → NDCPicture
    removenameNDCP: NameSet SelectCrit NDCPicture → NDCPicture
    addnameNDCP: NameSet SelectCrit NDCPicture → NDCPicture
    deleteNDCP: SelectCrit NDCPicture → NDCPicture
    renameNDCP: Name Name SelectCrit NDCPicture → NDCPicture
    selectpicture: NDCPicture SelectCrit → NDCPicture
    lastp: NDCPicture → NameSet
    getfirst: NDCPicture SelectCrit → NameSet
    getlast: NDCPicture SelectCrit → NameSet
    insert: NDCPicture NDCPicture SelectCrit Position → NDCPicture
vars ndcp, ndcp1:NDCPicture
    ns,ns1:NameSet
    n,on,nn:Name
    Selcrit:SelectCrit
    pp:PicturePart
    lndcp: ListofNDCP
    pli,pli1: PlInd
    asf,asf1: asfs
    lt,lt1: Linetype
    lw,lw1: Linewidth
    sa: Source
    la: Logical

```

ndc: NDCattr
position: Position

eqns (*appendNDCP(emptyNDCP, ndcp) = ndcp*)
*(appendNDCP(addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
sourcea(asf,pli),la),ndcp), ndcpI)*
*= addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
sourcea(asf,pli),la), appendNDCP(ndcp,ndcpI)))*

(setattrNDCP(Selcrit,pli1,emptyNDCP) = emptyNDCP)
*(setattrNDCP(Selcrit,pli1,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
sourcea(asf,pli),la),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc,
sourcea(asf,pli),la),setattrNDCP(Selcrit,pli1,ndcp))*
IF (satisfy(ns,Selcrit)==T))
*(setattrNDCP(Selcrit,pli1,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
sourcea(asf,pli),la), ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns),ndc,
sourcea(asf,pli),la),setattrNDCP(Selcrit,pli1,ndcp))*
IF (satisfy(ns,Selcrit)==F))
(setattrNDCP(Selcrit,asf1,emptyNDCP) = emptyNDCP)
*(setattrNDCP(Selcrit,asf1,addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc,
sourcea(asf,pli),la),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc,
sourcea(asf,pli),la), setattrNDCP(Selcrit,asf1,ndcp))*
IF (satisfy(ns,Selcrit)==T))
*(setattrNDCP(Selcrit,asf1,addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc,
sourcea(asf,pli),la),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc,
sourcea(asf,pli),la), setattrNDCP(Selcrit,asf1,ndcp))*
IF (satisfy(ns,Selcrit)==F))
(setattrNDCP(Selcrit,lt1,emptyNDCP) = emptyNDCP)
*(setattrNDCP(Selcrit,lt1,addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)),setattrNDCP(Selcrit,lt1,ndcp))*
IF (satisfy(ns,Selcrit)==T))
*(setattrNDCP(Selcrit,lt1,addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)), ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)), setattrNDCP(Selcrit,lt1,ndcp))*
IF (satisfy(ns,Selcrit)==F))
(setattrNDCP(Selcrit,lw1,emptyNDCP) = emptyNDCP)
*(setattrNDCP(Selcrit,lw1,addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)),setattrNDCP(Selcrit,lw1,ndcp))*
IF (satisfy(ns,Selcrit)==T))
*(setattrNDCP(Selcrit,lw1,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,
logicala(lt,lw)),ndcp))*
*= addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,
logicala(lt,lw)), setattrNDCP(Selcrit,lw1,ndcp))*
IF (satisfy(ns,Selcrit)==F))

(addnameNDCP(ns1,Selcrit,emptyNDCP) = emptyNDCP)

```

(addnameNDCP(ns1,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp,identifa((ns)U(ns1)), ndc, sa,la),
 addnameNDCP(ns1,Selcrit,ndcp))
 IF (satisfy(ns,Selcrit)==T))
(addnameNDCP(ns1,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,la),
 addnameNDCP(ns1,Selcrit,ndcp))
 IF not (satisfy(ns,Selcrit)==T))

(removenameNDCP(ns1,Selcrit,emptyNDCP) = emptyNDCP)
(removenameNDCP(ns1,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp, identifa(subtractset(ns1,ns)), ndc, sa, la),
 removenameNDCP(ns1,Selcrit,ndcp))
 IF (satisfy(ns,Selcrit)==T))
(removenameNDCP(ns1,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa, la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,la),
 removenameNDCP(ns1,Selcrit,ndcp))
 IF not (satisfy(ns,Selcrit)==T))

(deleteNDCP(Selcrit,emptyNDCP) = emptyNDCP)
(deleteNDCP(Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = deleteNDCP(Selcrit,ndcp) IF (satisfy(ns,Selcrit)==T))
(deleteNDCP(Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la), deleteNDCP(Selcrit,ndcp))
 IF (satisfy(ns,Selcrit)==F))

(renameNDCP(on,nn,Selcrit,emptyNDCP) = emptyNDCP)
(renameNDCP(on,nn,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa,la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp, identifa(rename(nn,nn,ns)), ndc, sa, la),
 renameNDCP(on,nn,Selcrit,ndcp)) IF satisfy(ns,Selcrit))
(renameNDCP(on,nn,Selcrit,addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa, la),ndcp))
 = addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa, la),
 renameNDCP(on,nn,Selcrit,ndcp)) IF not satisfy(ns,Selcrit))

(selectpicture(emptyNDCP,Selcrit) = emptyNDCP)
(selectpicture(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la),ndcp), Selcrit)
 = addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,la), selectpicture(ndcp,Selcrit))
 IF (satisfy(ns,Selcrit)==T))
(selectpicture(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa,la),ndcp), Selcrit)
 = selectpicture(ndcp, Selcrit) IF not (satisfy(ns,Selcrit)==T))

(getfirst(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la),ndcp), Selcrit)
 = ns IF (satisfy(ns,Selcrit)==T))
(getfirst(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la),ndcp), Selcrit)
 = getfirst(ndcp, Selcrit) IF not (satisfy(ns,Selcrit)==T))

(getlast(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la),ndcp), Selcrit)
 = ns IF (satisfy(ns,Selcrit)==T) and
 (lastp(selectpicture(addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sa, la),ndcp), Selcrit))==ns))
(getlast(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndc, sa, la),ndcp), Selcrit)
 = getlast(ndcp, Selcrit)
 IF not (satisfy(ns,Selcrit)==T) or
 not (lastp(selectpicture(addNDCP(mkSetofPolyline(lndcp, identifa(ns),
 ndc, sa, la),ndcp), Selcrit))==ns))

```

```

(lastp(addNDCP(mkSetofPolyline(lndcp,identifa(ns),ndc,sa,la), ndcp)) = ns IF (ndcp==emptyNDCP))
(lastp(addNDCP(mkSetofPolyline(lndcp,identifa(ns),ndc,sa,la), ndcp)) = lastp(ndcp)
    IF not (ndcp==emptyNDCP))

(insert(emptyNDCP, ndcp, Selcrit, position) = ndcp)
(insert(ndcp1, addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sourcea(asf,pli),la),ndcp),
    Selcrit, FRONT)
= appendNDCP(ndcp1, addNDCP(mkSetofPolyline(lndcp, identifa(ns),
    ndc, sourcea(asf,pli),la), ndcp))
    IF (getfirst(addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
        sourcea(asf,pli),la),ndcp),Selcrit)==ns))
(insert(ndcp1, addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sourcea(asf,pli),la),ndcp),
    Selcrit, FRONT)
= addNDCP(mkSetofPolyline(lndcp,identifa(ns),
    ndc,sourcea(asf,pli),la),insert(ndcp1,ndcp,Selcrit,FRONT))
    IF not (getfirst(addNDCP(mkSetofPolyline(lndcp,identifa(ns),ndc,
        sourcea(asf,pli),la),ndcp),Selcrit)==ns))
(insert(ndcp1, addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sourcea(asf,pli),la),ndcp),
    Selcrit, BACK)
= addNDCP(mkSetofPolyline(lndcp,identifa(ns),
    ndc,sourcea(asf,pli),la), appendNDCP(ndcp1, ndcp))
    IF (getLast(addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
        sourcea(asf,pli),la),ndcp),Selcrit)==ns))
(insert(ndcp1, addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc, sourcea(asf,pli),la),ndcp),
    Selcrit, BACK)
= addNDCP(mkSetofPolyline(lndcp,identifa(ns),
    ndc,sourcea(asf,pli),la), insert(ndcp1, ndcp, Selcrit, BACK))
    IF not (getLast(addNDCP(mkSetofPolyline(lndcp, identifa(ns), ndc,
        sourcea(asf,pli),la),ndcp),Selcrit)==ns))

```

jbo

3.13. PPNDCCONVERTER

This object describes the operations which copy a picture part into the NDC picture and copy a portion of the NDC picture into a picture part.

```

obj  PPNDCCONVERTER / NDCPICTURE
sorts
ops  copyPPNDCP: PicturePart SelectCrit Matrix23 TransMode
      Matrix23 TransMode NameSet NDCPicture → NDCPicture
      copyNDCPPP: NDCPicture → PicturePart
vars sply: SetofPolyline
      ndcp:NDCPicture
      ns,ns1:NameSet
      n,on,nn:Name
      Selcrit:SelectCrit
      pp:PicturePart
      lndcp: ListofNDCP
      pli,pli1: PlInd
      asf,asf1: asfs
      lt,lt1: Linetype
      lw,lw1: Linewidth
      sa: Source
      la: Logical
      ndc: NDCattr

```

```

global,local: Matrix23
trmode,trmode1: TransMode
eqns (copyPPNDCP(emptyPP,Selcrit,global,trmode,local,trmode1,ns,ndcp)=ndcp)
      (copyPPNDCP(addPP(mkSetofPolyline(lndcp, identifa(ns1), ndc, sa,la), pp),
                   Selcrit, global, trmode, local, trmode1, ns, ndcp)
       = addNDCP(mkSetofPolyline(lndcp, identifa((ns1)U(ns)),
                                  modifyndca(global, trmode, local, trmode1, ndc), sa,la),
                  copyPPNDCP(pp,Selcrit,global,trmode,local,trmode1,ns,ndcp))
       IF (satisfy(ns1 ,Selcrit)==T))
      (copyPPNDCP(addPP(mkSetofPolyline(lndcp, identifa(ns1), ndc, sa, la), pp),
                   Selcrit, global, trmode, local, trmode1, ns, ndcp)
       = copyPPNDCP(pp,Selcrit,global,trmode,local,trmode1,ns,ndcp)
       IF (satisfy(ns1 ,Selcrit)==F))
      (copyNDCPPP(emptyNDCP) = emptyPP)
      (copyNDCPPP(addNDCP(sply,ndcp)) = addPP(sply,copyNDCPPP(ndcp)))
jbo

```

3.14. VIEW and LISTOFVW

VIEW describes views. A view consists of a selection criterion and a transformation matrix. *LISTOFVW* describes a list of view transformations and is used in describing the workstation state list.

```

obj  VIEW /SELECTION MATRIX23
sorts View ViewInd
ops  mkView: SelectCrit Matrix23 Matrix23 → View
      sets: SelectCrit View → View
      seta: Matrix23 Matrix23 View → View
      VWNO: → ViewInd
      VWN1: → ViewInd
      VWN2: → ViewInd
      VWN3: → ViewInd
      SELCRIT: → SelectCrit
      SELCRITI: → SelectCrit
      VWT: → Matrix23
      VWT1: → Matrix23
vars viewsel, viewsel1: SelectCrit
      omatrix, mmatrix, omatrix1, mmatrix1: Matrix23
eqns (sets(viewsel1, mkView(viewsel, omatrix, mmatrix))
      = mkView(viewsel1, omatrix, mmatrix))
      (seta(omatrix1, mmatrix1, mkView(viewsel, omatrix, mmatrix))
      = mkView(viewsel, omatrix1, mmatrix1))
jbo

```

```

image
  (TABLE => LISTOFVW) / VIEW
sorts (tb => ListofVW)
  (telem => View)
  (index => ViewInd)
ops  (emptyTb: → tb => emptyLVW)
endim

```

3.15. PLBUNDLETABLE

This object describes polyline bundle tables.

```
image
  (TABLE => PLBUNDLETABLE) /ATTRIBUTES
sorts (tb => PlBunTab)
  (telem => PlBun)
  (index => PlInd)
ops (emptyTb: → tb => emptyBt)
endim
```

3.16. WSL

This object describes the Workstation State List.

```
obj  WSL / SELECTION PLBUNDLETABLE LISTOFVW
sorts wsl VisEffSt
ops  MATRIX23: → Matrix23
    ALLOW, SUPPRESS: → VisEffSt
    mkWSL: PlBunTab ListofVW Matrix23 VisEffSt SelectCrit SelectCrit SelectCrit →wsl
jbo
```

3.17. LDCPOINT, LDCPOINTS, LISTOFLDCPOINTS

These objects describe points and lists of points in LDC space. The transformation from lists of points in NDC to lists of points in LDC is also defined.

```
obj  LDCPOINT /NDCPOINT
sorts LDCPoint
ops  mkLDCPoint: int int → LDCPoint
    transfMapping: NDCPoint Matrix23 → LDCPoint
    transfVW: NDCPoint Matrix23 Matrix23 → LDCPoint
vars x,y,a,b,c,d,e,f: int
  a1,b1,c1,d1,e1,f1: int
eqns (transfMapping(mkNDCPoint(x,y),mktransfcor(a,b,c,d,e,f))
      = mkLDCPoint((x*a)+(y*b)+c, (x*d)+(y*e)+f))
  (transfVW(mkNDCPoint(x,y), mktransfcor(a,b,c,d,e,f), mktransfcor(a1,b1,c1,d1,e1,f1))
   = transfMapping(transfNDC(mkNDCPoint(x,y), mktransfcor(a,b,c,d,e,f)),
                  mktransfcor(a1,b1,c1,d1,e1,f1)))
jbo

obj  LDCPOINTS /NDCPOINTS LDCPOINT
sorts LDCPoints
ops  emptyLDCPoints: → LDCPoints
    addLDCpoint: LDCPoint LDCPoints → LDCPoints
    transfVWPoints: NDCPoints Matrix23 Matrix23 → LDCPoints
vars pn: NDCPoint
  pnts: NDCPoints
  mat, mat1: Matrix23
eqns (transfVWPoints(emptyNDCPoints, mat, mat1) = emptyLDCPoints)
  (transfVWPoints(addNDCpoint(pn,pnts), mat, mat1)
   = addLDCpoint(transfVW(pn,mat, mat1), transfVWPoints(pnts,mat, mat1)))
jbo

obj  LISTOFLDCPOINTS /LDCPOINTS LISTOFTNDCPOINTS
sorts ListofLDCP
```

```

ops emptyLofLDCP: → ListofLDCP
    addLDCpoints: LDCPoints ListofLDCP → ListofLDCP
    transfVWLofPoints: ListofNDCP Matrix23 Matrix23 → ListofLDCP
vars pnts: NDCPoints
    lopnts: ListofNDCP
    mat, mat1: Matrix23
eqns (transfVWLofPoints(emptyLofNDCP, mat, mat1) = emptyLofLDCP)
    (transfVWLofPoints(addNDCpoints(pnts, lopnts), mat, mat1)
     = addLDCpoints(transfVWPoints(pnts, mat, mat1), transfVWLofPoints(lopnts, mat, mat1)))
jbo

```

3.18. SETOFLGPOLYLINE, LOGICALPICTURE

These objects describe the set of polyline primitive in the logical picture and the logical picture itself, together with the operations to transform the NDC picture to the logical picture.

```

obj SETOFLGPOLYLINE /ATTRIBUTES LISTOFLDCPOINTS
sorts SofLOGPolyline
ops mkSofLOGPolyline: ListofLDCP Identification Logical Highl Det → SofLOGPolyline
jbo

```

```

obj LOGICALPICTURE /SETOFLGPOLYLINE PPNDCCONVERTER WSL
sorts LOGPicture
ops emptyLOGP: → LOGPicture
    addLOGP: SofLOGPolyline LOGPicture → LOGPicture
    appendLOGP: LOGPicture LOGPicture → LOGPicture
    applyvt: NDCPicture View PlBunTab SelectCrit SelectCrit → LOGPicture
    applyviews: NDCPicture ListofVW PlBunTab SelectCrit SelectCrit → LOGPicture
vars i: ViewInd
    Selcrit, sh, sd: SelectCrit
    omatrix, mmatrix: Matrix23
    vw: View
    lvw1, lvw2: ListofVW
    ntcp, ntcp1: LOGPicture
    ndcp: NDCPicture
    ns: NameSet
    lndcp: ListofNDCP
    pp: SofLOGPolyline
    sa: Source
    la: Logical
    local, global: Matrix23
    pli: PlInd
    pbt: PlBunTab
    a, al: ASF
    asf: asfs
    lt, blt: Linetype
    lw, blw: LineWidth
eqns (appendLOGP(emptyLOGP, ntcp) = ntcp)
    (appendLOGP(addLOGP(pp, ntcp), ntcp1) = addLOGP(pp, appendLOGP(ntcp, ntcp1)))

    (applyvt(emptyNDCP, vw, pbt, sh, sd) = emptyLOGP)
    (applyvt(addNDCP(mkSetofPolyline(lndcp, identifa(ns)), ndca(local, global),
        sourcea(asf, pli), la), ndcp), mkView(Selcrit, omatrix, mmatrix), pbt, sh, sd)
     = addLOGP(mkSofLOGPolyline(transfVWLofPoints(
        transfLofNDCPoints(transfLofNDCPoints(lndcp, local), global), omatrix, mmatrix),
        transfLofNDCPoints(transfLofNDCPoints(lndcp, local), global), omatrix, mmatrix)),

```

```

identifa(ns),
selectclogattr(asf,la,pbt [ pli ],highlt(ns,sh),dec1(ns,sd)),
applyvt(ndcp,mkView(Selcrit,omatrix,mmatrix),pbt,sh,sd))
    IF satisfy(ns,Selcrit))
(applyvt(addNDCP(mkSetofPolyline(lndcp,identifa(ns), ndca(local, global),
sourcea(asf,pli),la), ndcp), mkView(Selcrit,omatrix,mmatrix),pbt,sh,sd)
= applyvt(ndcp,mkView(Selcrit,omatrix,mmatrix),pbt,sh,sd)
    IF not (satisfy(ns,Selcrit)))
(applyviews(emptyNDCP, lww1, pbt, sh, sd) = emptyLOGP)
(applyviews(ndcp, (lww1)U(lww2), pbt, sh, sd)
= appendLOGP(applyviews(ndcp, lww1, pbt, sh, sd), applyviews(ndcp, lww2, pbt, sh, sd))
    IF not (ndcp==emptyNDCP))
(applyviews(ndcp, (i % vw), pbt, sh, sd) = applyvt(ndcp,vw,pbt,sh,sd))
jbo

```

3.19. DCPOINT, DCPOINTS, LISTOFCPOINTS, SETOFRFPOLYLINE

These objects describe points, lists of points and the set of polyline primitive in the reified picture.

```

obj DCPOINT / LDCPOINT MATRIX23
sorts DCPoint
ops mkDCPoint: int int → DCPoint
    transfWS: LDCPoint Matrix23 → DCPoint
vars x,y,a,b,c,d,e,f: int
eqns (transfWS(mkLDCPoint(x,y),mktransfcor(a,b,c,d,e,f))
      = mkDCPoint((x*a)+(y*b)+c, (x*d)+(y*e)+f))
jbo

```

```

obj DCPOINTS /LDCPOINTS DCPOINT
sorts DCPoints
ops emptyDCPoints: → DCPoints
    addDCpoint: DCPoint DCPoints → DCPoints
    transfWSPoints: LDCPoints Matrix23 → DCPoints
vars pn: LDCPoint
    pnts: LDCPoints
    mat: Matrix23
eqns (transfWSPoints(emptyLDCPoints, mat) = emptyDCPoints)
    (transfWSPoints(addLDCpoint(pn,pnts), mat)
     = addDCpoint(transfWS(pn,mat), transfWSPoints(pnts,mat)))
jbo

```

```

obj LISTOFCPOINTS /DCPOINTS LISTOFLDCPOINTS
sorts ListofDCP
ops emptyLofDCP: → ListofDCP
    addDCpoints: DCPoints ListofDCP → ListofDCP
    transfWSLofPoints: ListofLDCP Matrix23 → ListofDCP
vars pnts: LDCPoints
    lopnts: ListofLDCP
    mat: Matrix23
eqns (transfWSLofPoints(emptyLofDCP, mat) = emptyLofDCP)
    (transfWSLofPoints(addLDCpoints(pnts,lopnts), mat)
     = addDCpoints(transfWSPoints(pnts,mat),transfWSLofPoints(lopnts,mat)))
jbo

```

```
obj SETOFRFPOLYLINE /ATTRIBUTES LISTOFCPOINTS
sorts SofRFPolyline
ops mkSofRFPolyline: ListofDCP Identification Logical Highl Det → SofRFPolyline
jbo
```

3.20. WINDOWSANDVIEWPORTS

This object describes the workstation window and viewport and a simplified specification of the workstation transformation (the isotropic nature of this transformation is not described here).

```
obj WINDOWSANDVIEWPORTS /NDCPOINT DCPOINT
sorts WCWin NDCVp LDCWin DCVp
ops mkWCWin: WCPoint WCPoint → WCWin
    mkNDCVp: NDCPoint NDCPoint → NDCVp
    mkLDCWin: NDCPoint NDCPoint → LDCWin
    mkDCVp: DCPoint DCPoint → DCVp
    gettransfNT: int int int int int int int → Matrix23
    gettransfWS: int int int int int int int → Matrix23
    WSW: → LDCWin
    WSV: → DCVp
vars xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2: int
eqns (gettransfNT(xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2)
      = mktransfcor(((xv2-xv1) div (xw2-xw1)),ps 0,xv1-xw1,ps 0,
                    ((yv2-yv1) div (yw2-yw1)),yv1-yw1))
  (gettransfWS(xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2)
      = mktransfcor(((xv2-xv1) div (xw2-xw1)),ps 0,xv1-xw1,ps 0,
                    ((yv2-yv1) div (yw2-yw1)),yv1-yw1))
jbo
```

3.21. GSL

This object describes the GKS State List.

```
obj GSL /NAMESETS LISTOFTN ATTRIBUTES WINDOWSANDVIEWPORTS
sorts gsl
ops mkGSL: NameSet NameSet Matrix23 Matrix23 PlInd asfs
    Linetype Linewidth NormTran ListofNT PicPartName → gsl
    addnt: NormTran WCWin NDCVp gsl → gsl
    getPicPartName: gsl → PicPartName
vars xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2: int
    opw,ns: NameSet
    pli: PlInd
    asf: asfs
    local, global: Matrix23
    ltype: Linetype
    lw: Linewidth
    ntn,ntn1: NormTran
    ntl: ListofNT
    pn: PicPartName
eqns (addnt (ntn1,mkWCWin(mkWCPoint(xw1,yw1),mkWCPoint(xw2,yw2)),
      mkNDCVp(mkNDCPoint(xv1,yv1),mkNDCPoint(xv2,yv2)),
      mkGSL(opw,ns,local,global,pli,asf,ltype,lw,ntn,ntl,pn))
      = mkGSL(opw,ns,local,global,pli,asf,ltype,lw,ntn,
        (ntl + (ntn1 % (gettransfNT(xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2)))),pn)) IF not (ntn1==NTN0))
  (getPicPartName(mkGSL(opw,ns,local,global,pli,asf,ltype,lw,ntn,ntl,pn)) = pn)
jbo
```

3.22. REIFIEDPICTURE

This object describes the reified picture and the transformation from the logical picture to the reified picture.

```
obj REIFIEDPICTURE /SETOFRFPOLYLINE LOGICALPICTURE
sorts REIFPicture
ops emptyRFP: → REIFPicture
      addRFP: SofRFPolyline REIFPicture → REIFPicture
      logptoreifp: LOGPicture Matrix23 REIFPicture → REIFPicture
vars wst: Matrix23
      soflogp: SofLOGPolyline
      lnpfp: ListofLDCP
      logp: LOGPicture
      ia: Identification
      la: Logical
      h: Highl
      d: Det
eqns (logptoreifp(emptyLOGP,wst) = emptyRFP)
      (logptoreifp(addLOGP(mkSofLOGPolyline(lnpcp,ia,la,h,d),logp),wst)
       = addRFP(mkSofRFPolyline(transfWSLOfPoints(lnpcp,wst),ia,la,h,d),
                 logptoreifp(logp,wst)))
jbo
```

3.23. WORKSTATIONS

This object describes workstations and the operations on them.

```
obj WORKSTATIONS / REIFIEDPICTURE WINDOWSANDVIEWPORTS
sorts Workstations
OPS mkWSs: WsId REIFPicture wsl → Workstations
emptyWorkstations: → Workstations
U : Workstations Workstations → Workstations (ASSOC COMM ID:emptyWorkstations)
OpenWS: WsId Workstations → Workstations
updatereifp: NDCPicture VisEffSt SelectCrit SelectCrit SelectCrit
            PlBunTab ListofVW Matrix23 REIFPicture → REIFPicture

DisplayNDCPWorkstations: NDCPicture Workstations → Workstations
DisplayNDCPWs: WsId NDCPicture Workstations → Workstations

deleteWs: WsId Workstations → Workstations
setsdis: WsId NDCPicture SelectCrit Workstations → Workstations
setsh: WsId NDCPicture SelectCrit Workstations → Workstations
setsd: WsId NDCPicture SelectCrit Workstations → Workstations
setEffects: WsId VisEffSt NDCPicture Workstations → Workstations
setrep: WsId PlInd PlBun NDCPicture Workstations → Workstations
setviewrep: WsId ViewInd Matrix23 Matrix23 NDCPicture Workstations → Workstations
setviewsel: WsId ViewInd SelectCrit NDCPicture Workstations → Workstations
setwandvw: WsId LDCWin DCVp NDCPicture Workstations → Workstations
vars wkstns,wkstns1,wkstns2:Workstations
wsid,wsid1:WsId
ns,ns1,acw,awi ,vs,hs,ds:NameSet
ndcp:NDCPicture
reifp:REIFPicture
wsl: wsl
Selcrit,s,sdis,sdis1,sh,sh1,sd,sd1,viewsel,viewsell:SelectCrit
pp:PicturePart
```

```

 $vef, vef1 : VisEffSt$ 
 $pbt : PlBunTab$ 
 $bl : PlBun$ 
 $pli : PlInd$ 
 $vwl : ListofVW$ 
 $vwn : ViewInd$ 
 $view : View$ 
 $wst, omatrix, mmatrix, omatrixl, mmatrixl : Matrix23$ 
 $wsww : LDCWin$ 
 $wsvw : DCVp$ 
 $xw1, yw1, xw2, yw2, xv1, yv1, xv2, yv2 : int$ 
 $h : Highl$ 
 $d : Det$ 
eqns ((wkstns)U(wkstns) = wkstns)

(OpenWS(wsid, wkstns)
= (mkWSs(wsid, emptyRFP,
  mkWSL(
    (PLI0 % mkBundle(DASHED, THICK)) U
    (PLI1 % mkBundle(DOTTED, MEDIUM)),
    (VWN0 % mkView(SELECTALL, mktransfcor(ps 1, ps 0, ps 0, ps 0, ps 1, ps 0),
      mktransfcor(ps 1, ps 0, ps 0, ps 0, ps 1, ps 0))) U
    (VWN1 % mkView(REJECTALL,
      mktransfcor(ps 1, ps 0, ps 0, ps 0, ps 1, ps 0),
      mktransfcor(ps 1, ps 0, ps 0, ps 0, ps 1, ps 0))),
      mktransfcor(ps 1, ps 0, ps 0, ps 0, ps 1, ps 0), ALLOW,
      SELECTALL, REJECTALL, REJECTALL))) U (wkstns))

(updatereifp(ndcp, SUPPRESS, sdis, sh, sd, pbt, vwl, wst, reifp) = reifp)
(updatereifp(ndcp, ALLOW, sdis, sh, sd, pbt, vwl, wst, reifp)
 = logtoreifp(applyviews(selectpicture(ndcp, sdis),
  vwl, pbt, sh, sd), wst))

(DisplayNDCPWorkstations(ndcp, emptyWorkstations) = emptyWorkstations)

(DisplayNDCPWorkstations(ndcp, (wkstns1) U (wkstns2))
= (DisplayNDCPWorkstations(ndcp, wkstns1)) U
(DisplayNDCPWorkstations(ndcp, wkstns2)))
(DisplayNDCPWorkstations(ndcp, mkWSs(wsid, reifp,
  mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 = mkWSs(wsid, updatereifp(ndcp, vefs, dis, sh, sd, pbt, vwl, wst, reifp), mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
(DisplayNDCPWs(wsid, ndcp, emptyWorkstations) = emptyWorkstations)
(DisplayNDCPWs(wsid, ndcp, (wkstns1) U (wkstns2))
 = (DisplayNDCPWs(wsid, ndcp, wkstns1)) U
(DisplayNDCPWs(wsid, ndcp, wkstns2)))
(DisplayNDCPWs(wsid, ndcp,
  mkWSs(wsid, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 = mkWSs(wsid, updatereifp(ndcp, vef, sdis, sh, sd, pbt, vwl, wst, reifp), mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
(DisplayNDCPWs(wsid, ndcp, mkWSs(wsid1, reifp, wksl))
 = mkWSs(wsid1, reifp, wksl) IF not (wsid == wsid1))

(deleteWs(wsid, emptyWorkstations) = emptyWorkstations)
(deleteWs(wsid, (wkstns1) U (wkstns2))
 = (deleteWs(wsid, wkstns1)) U (deleteWs(wsid, wkstns2)))

```



```

(setviewrep(wsid, vwn, omatrix, mmatrix, ndcp, emptyWorkstations)
 =emptyWorkstations)
(setviewrep(wsid,vwn,omatrix,mmatrix,ndcp,(wkstns1) U (wkstns2))
 =(setviewrep(wsid,vwn,omatrix,mmatrix,ndcp,wkstns1)) U
 (setviewrep(wsid,vwn,omatrix,mmatrix,ndcp,wkstns2)))
(setviewrep(wsid,vwn,omatrix1,mmatrix1,ndcp,mkWSS(wsidi,reifp,
 mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi,
 updatereifp(ndcp, vef, sdis, sh, sd, pbt, vwl + (vwn % seta(omatrix1, mmatrix1, vwl [ vwn ])), wst, reifp),
 mkWSL(pbt, vwl + (vwn % seta(omatrix1, mmatrix1, vwl [ vwn ])),wst, vef, sdis, sh, sd)))

(setviewrep(wsid1, vwn, omatrix1, mmatrix1, ndcp,
 mkWSS(wsidi, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd))
 IF not (wsidl==wsid)
(setviewsel(wsid, vwn, viewsel, ndcp, emptyWorkstations) = emptyWorkstations)
(setviewsel(wsid, vwn, viewsel, ndcp, (wkstns1) U (wkstns2))
 =(setviewsel(wsid, vwn, viewsel, ndcp, wkstns1)) U (setviewsel(wsid, vwn, viewsel, ndcp, wkstns2)))
(setviewsel(wsid, vwn, viewsel1, ndcp, mkWSS(wsidi, reifp,
 mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi, updatereifp(ndcp, vef, sdis, sh, sd, pbt, vwl + (vwn % sets(viewsel1, vwl [ vwn ])), wst, reifp),
 mkWSL(pbt, vwl + (vwn % sets(viewsel1, vwl [ vwn ])), wst, vef, sdis, sh, sd)))
(setviewsel(wsid1, vwn, viewsel1, ndcp, mkWSS(wsidi, reifp,
 mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd))
 IF not (wsidl==wsid))

(setwwandvw(wsidi,wsww,wsvw,ndcp,emptyWorkstations) = emptyWorkstations)
(setwwandvw(wsidi, wsww, wsvw, ndcp, (wkstns1) U (wkstns2))
 =(setwwandvw(wsidi, wsww, wsvw, ndcp, wkstns1)) U (setwwandvw(wsidi, wsww, wsvw, ndcp, wkstns2)))
(setwwandvw(wsidi, mkLDCWin(mkNDCCPoint(xw1, yw1),
 mkNDCCPoint(xw2, yw2)), mkDCVp(mkDCPoint(xv1, yv1),
 mkDCPoint(xv2, yv2)), ndcp, mkWSS(wsidi, reifp,
 mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi, updatereifp(ndcp, vef, sdis, sh, sd, pbt, vwl,
 gettransfWS(xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2), reifp),
 mkWSL(pbt, vwl, gettransfWS(xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2),
 vef, sdis, sh, sd)))

(setwwandvw(wsidi1, wsww, wsvw, ndcp, mkWSS(wsidi, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd)))
 =mkWSS(wsidi, reifp, mkWSL(pbt, vwl, wst, vef, sdis, sh, sd))
 IF not (wsidl==wsid))

```

jbo

3.24. GKS

This is the top object in the object hierarchy which describes the GKS-9x functions.

```

obj GKS / GSL PICTUREPARTSTORE WORKSTATIONS
sorts gks
ops mkGKS: gsl PPS NDCPicture Workstations → gks
      OpenGKS: → gks
      CreateOutputPrim: ListofWCP gks → gks
      SetPrimitiveAttribute: P1Ind gks → gks
      SetPrimitiveAttribute: asfs gks → gks

```

SetPrimitiveAttribute: Linetype gks → gks
SetPrimitiveAttribute: Linewidth gks → gks
AddSetofNamestoNameSet: NameSet gks → gks
RemoveSetofNamesfromNameSet: NameSet gks → gks

SetWindowandViewport: NormTran WCWin NDCVp gks → gks
SetNormTranNumber: NormTran gks → gks

DeletePrimitives: SelectCrit gks → gks
RemoveSetofNamesfromNDCP: NameSet SelectCrit gks → gks
AddSetofNamestoNDCP: NameSet SelectCrit gks → gks
ReorderNDCPicture: SelectCrit SelectCrit Position gks → gks
SetNDCPictureAttribute: SelectCrit PlInd gks → gks
SetNDCPictureAttribute: SelectCrit asfs gks → gks
SetNDCPictureAttribute: SelectCrit Linetype gks → gks
SetNDCPictureAttribute: SelectCrit Linewidth gks → gks

BeginPicturePart: PicPartName gks → gks
EndPicturePart: gks → gks
BeginPPPartAgain: PicPartName gks → gks
AppendPicturePart: PicPartName PicPartName Matrix23 TransMode
 Matrix23 TransMode NameSet gks → gks
RenamePicturePart: PicPartName PicPartName gks → gks
DeletePicturePart: PicPartName gks → gks
CopyPicturePartfromPPS: PicPartName SelectCrit Matrix23 TransMode
 Matrix23 TransMode NameSet gks → gks
CopyNDCPicturetoPPS: SelectCrit PicPartName NameSet gks → gks

OpenWorkstation: WsId gks → gks
CloseWorkstation: WsId gks → gks
SetRepresentation: WsId PlInd PlBun gks → gks
SetView: WsId ViewInd Matrix23 Matrix23 gks → gks
SetViewSelCriterion: WsId ViewInd SelectCrit gks → gks
SetNDCVisualEffects: WsId VisEffSt gks → gks
SetWSWindowandViewport: WsId LDCWin DCVp gks → gks
SetWsSelCriterion: WsId SelectDisp SelectCrit gks → gks
SetWsSelCriterion: WsId SelectHighl SelectCrit gks → gks
SetWsSelCriterion: WsId SelectDet SelectCrit gks → gks

TrNT1: → Matrix23
TrNT0: → Matrix23

vars *gks1 :gks*
n: Name
ns,ns1,awi,opw,acw,usn,usn1,usn2,vs,hs,ds: NameSet
p: SetofPolyline
pps,pps1,pps2: PPS
pn,pn1,pn2: PicPartName
pp: PicturePart
ndcp: NDCPicture
reifp: REIFPicture
gsl1: gsl
wkstns: Workstations
vwn: ViewInd
view: View

```

wksl: wsl
Selcrit, Selcrit1 ,sdis,sh,sh,viewsel: SelectCrit
omatrix, mmatrix: Matrix23
vef,vef1: VisEffSt
pli,pli1: PlInd
bl: PlBun
asf: asfs
ndc: NDCattr
local, global,local1, global1: Matrix23
trmode,trmode1: TransMode
ltype,ltype1: Linetype
lw,lw1: Linewidth
ntn,ntn1: NormTran
ntl: ListofNT
las,las1 ,was,was1: ASF
ww: WCWin
vw: NDCVp
wsww: LDCWin
wsvw: DCVp
xw1,yw1,xw2,yw2,xv1,yv1,xv2,yv2: int
lofwcp: ListofWCP
lofndcp: ListofNDCP
h: Highl
d: Det
wsid,wsid1: WsId
position: Position
eqns (OpenGKS
      = mkGKS(mkGSL(emptyNS, emptyNS,
                      mktransfcor(ps 1,ps 0,ps 0,ps 0,ps 1,ps 0),
                      mktransfcor(ps 1,ps 0,ps 0,ps 0,ps 1,ps 0),
                      PLIO, asfsa(BUNDLED, INDIVIDUAL), SOLID, THIN, NTN0,
                      ((NTN0 % mktransfcor(ps 1,ps 0,ps 0,ps 0,ps 1,ps 0)) U
                       (NTNI % mktransfcor(ps 2,ps 0,ps 0,ps 0,ps 2,ps 0))),
                      NONAMEPN),emptyPPS,emptyNDCP,emptyWorkstations))
      (CreateOutputPrim(lofwcp,mkGKS(mkGSL(opw,ns,local, global,pli,asf,
                                              ltype, lw,ntn,ntl,NONAMEPN),pps,ndcp,wkstns))
       = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,NONAMEPN),pps,
              addNDCP(mkSetofPolyline(transfLofPoints(lofwcp,ntl [ ntn ]),identifa(ns), ndca(local, global),
              sourcea(asf,pli), logicala(ltype,lw)), ndcp),
              DisplayNDCPWorkstations(addNDCP(mkSetofPolyline(transfLofPoints(lofwcp,ntl [ ntn ]),
              identifa(ns), ndca(local, global),
              sourcea(asf,pli), logicala(ltype,lw)), ndcp), wkstns)))
      (CreateOutputPrim(lofwcp,mkGKS(mkGSL(opw,ns,local, global,pli,
                                              asf,ltype, lw,ntn,ntl,pn),pps,ndcp, wkstns))
       = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),
              addtoPP(pn,mkSetofPolyline(transfLofPoints(lofwcp,ntl [ ntn ]),identifa(ns), ndca(local, global),
              sourcea(asf,pli),logicala(ltype,lw)),pps),
              ndcp, wkstns) IF not (pn == NONAMEPN))
      (SetPrimitiveAttribute(pli1, mkGKS(mkGSL(opw,ns,local, global,pli,
                                              asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
       = mkGKS(mkGSL(opw,ns,local,global,pli1,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
      (SetPrimitiveAttribute(asfsa(las1,was1), mkGKS(mkGSL(opw,ns,local,
                                              global,pli, asfsa(las,was),ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
       = mkGKS(mkGSL(opw,ns,local,global,pli,asfsa(las1,was1),ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))

```

```

(SetPrimitiveAttribute(ltype1,mkGKS(mkGSL(opw,ns,local,global,pli,
    asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype1,lw,ntn,ntl,pn),pps,ndcp,wkstns))
(SetActiveAttribute(lw1, mkGKS(mkGSL(opw,ns,local, global,pli,
    asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw1,ntn,ntl,pn),pps,ndcp,wkstns))
(AddSetofNamesToNameSet(ns1,mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,(ns) U (ns1),local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
(RemoveSetofNamesFromNameSet(ns1,mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,subtractset(ns1,ns),local,global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
(SetWindowAndViewport(ntn1,
    mkWCWin(mkWCPoint(xw1,yw1),mkWCPoint(xw2,yw2)),
    mkNDCVp(mkNDCPoint(xv1,yv1),mkNDCPoint(xv2,yv2)),
    mkGKS(gsl1,pps,ndcp,wkstns))
 = mkGKS(addnt(ntn1,mkWCWin(mkWCPoint(xw1,yw1),mkWCPoint(xw2,yw2)),
    mkNDCVp(mkNDCPoint(xv1,yv1),mkNDCPoint(xv2,yv2)),gsl1),
    pps,ndcp,wkstns) IF not ntn1==NTN0)
(SetNameTranNumber(ntn1,mkGKS(mkGSL(opw,ns,local,global,pli,asf,ltype,lw,
    ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local,global,pli,asf,ltype,lw,ntn1,ntl,pn),pps,ndcp,wkstns))
(DeletePrimitives(Selcrit, mkGKS(gsl1,pps,ndcp,wkstns))
 = mkGKS(gsl1,pps, deleteNDCP(Selcrit, ndcp),
    DisplayNDCPWorkstations(deleteNDCP(Selcrit,ndcp),wkstns)))
(RemoveSetofNamesFromNDCP(ns,Selcrit,mkGKS(gsl1 ,pps, ndcp, wkstns))
 = mkGKS(gsl1 ,pps,removenameNDCP(ns,Selcrit,ndcp),
    DisplayNDCPWorkstations(removenameNDCP(ns,Selcrit,ndcp),wkstns)))
(AddSetofNamesToNDCP(ns,Selcrit,mkGKS(gsl1 ,pps,ndcp,wkstns))
 = mkGKS(gsl1 ,pps,addnameNDCP(ns,Selcrit,ndcp),
    DisplayNDCPWorkstations(addnameNDCP(ns,Selcrit,ndcp),wkstns)))

(SetNDCPictureAttribute(Selcrit, pli1 ,
    mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,
    setattrNDCP(Selcrit,pli1,ndcp),
    DisplayNDCPWorkstations(setattrNDCP(Selcrit,pli1,ndcp),wkstns)))
(SetNDCPictureAttribute(Selcrit, asfsa(las1,was1),
    mkGKS(mkGSL(opw,ns,local, global,pli, asf,ltype, lw, ntn, ntl, pn),pps, ndcp, wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,
    setattrNDCP(Selcrit, asfsa(las1,was1),ndcp),
    DisplayNDCPWorkstations(setattrNDCP(Selcrit,asfsa(las1,was1),ndcp),wkstns)))
(SetNDCPictureAttribute(Selcrit, ltype1 ,
    mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,
    setattrNDCP(Selcrit,ltype1,ndcp),
    DisplayNDCPWorkstations(setattrNDCP(Selcrit,ltype1,ndcp),wkstns)))
(SetNDCPictureAttribute(Selcrit, lw1 ,
    mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,ndcp,wkstns))
 = mkGKS(mkGSL(opw,ns,local, global,pli,asf,ltype,lw,ntn,ntl,pn),pps,
    setattrNDCP(Selcrit,lw1,ndcp),
    DisplayNDCPWorkstations(setattrNDCP(Selcrit,lw1,ndcp),wkstns)))

(ReorderNDCPicture(Selcrit, Selcrit1 , position,mkGKS(gsl1,pps,ndcp,wkstns))
 = mkGKS(gsl1,pps, insert(selectpicture(ndcp, Selcrit),
    selectpicture(ndcp, snot(Selcrit)), Selcrit1 , position), wkstns)

```

```

    IF not (selectpicture(ndcp, sand(snot(Selcrit), Selcrit1)))
        == emptyNDCP))
(ReorderNDCPicture(Selcrit, Selcrit1, position, mkGKS(gsl1, pps, ndcp, wkstns))
= mkGKS(gsl1, pps, ndcp, wkstns)
    IF (selectpicture(ndcp, sand(snot(Selcrit), Selcrit1))
        == emptyNDCP))

(BeginPicturePart(pn1, mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn),
    pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn1),
    beginpicturepart(pn1, pps, ndcp, wkstns)
    IF (pn==NONAMEPN) and (PPisinPPS(pn1, pps)==F))
(BeginPPartAgain(pn1, mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, NONAMEPN),
    pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn1),
    pps, ndcp, wkstns)
    IF PPisinPPS(pn1, pps))
(EndPicturePart(mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn),
    pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, NONAMEPN),
    pps, ndcp, wkstns))
(AppendPicturePart(pn, pn1, global, trmode, local, trmode1, ns, mkGKS(gsl1, pps, ndcp, wkstns))
= mkGKS(gsl1, appendpicturepart(pn, pn1, global, trmode, local, trmode1, ns, pps), ndcp, wkstns)
    IF PPisinPPS(pn, pps) and PPisinPPS(pn1, pps))
(RenamePicturePart(pn, pn1,
    mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn2), pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn2),
    renamepicturepart(pn, pn1, pps), ndcp, wkstns)
    IF not (pn==NONAMEPN) and not (pn==pn2))
(RenamePicturePart(pn, pn1,
    mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn), pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn1),
    renamepicturepart(pn, pn1, pps), ndcp, wkstns)
    IF not (pn==NONAMEPN))
(RenamePicturePart(pn, pn1,
    mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, NONAMEPN), pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, NONAMEPN),
    renamepicturepart(pn, pn1, pps), ndcp, wkstns))
(DeletePicturePart(pn, mkGKS(gsl1, pps, ndcp, wkstns))
= mkGKS(gsl1, deletepicturepart(pn, pps), ndcp, wkstns))
(CopyPicturePartfromPPS(pn, Selcrit, global1, trmode, local1, trmode1, ns1,
    mkGKS(gsl1, pps, ndcp, wkstns))
= mkGKS(gsl1, pps, copyPPNDCP(getpicturepart(pn, pps), Selcrit, global1, trmode, local1, trmode1, ns1, ndcp),
    DisplayNDCPWorkstations(copyPPNDCP(getpicturepart(pn, pps),
        Selcrit, global1, trmode, local1, trmode1, ns1, ndcp), wkstns))
    IF not (getPicPartName(gsl1) == pn))
(CopyNDCPicturetoPPS(Selcrit, pn, ns1,
    mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn1), pps, ndcp, wkstns))
= mkGKS(mkGSL(opw, ns, local, global, pli, asf, ltype, lw, ntn, ntl, pn1),
    (mkPPS(pn, (copyNDCPPP(removenameNDCP(ns1, SELECTALL,
        selectpicture(ndcp, Selcrit))))))U(pps, ndcp, wkstns)
    IF not (pn1==pn))

(OpenWorkstation(wsid,

```

```

mkGKS(mkGSL(opw,ns,local,global,pli,ASF,ltype,lw,ntn,ntl,pnI),pps,ndcp,wkstns))
= mkGKS(mkGSL(addname(wsidtoname(wsid),opw),ns,local,global,pli,ASF,ltype,lw,ntn,ntl,pnI),
         pps,ndcp,
         DisplayNDCPWs(wsid,ndcp,OpenWS(wsid,wkstns))))
(CloseWorkstation(wsid,
                  mkGKS(mkGSL(opw,ns,local,global,pli,ASF,ltype,lw,ntn,ntl,pnI),pps,ndcp,wkstns))
                  = mkGKS(mkGSL(removessn(wsidtoname(wsid),opw),ns,local,global,pli,ASF,ltype,lw,ntn,ntl,pnI),
                           pps,ndcp,
                           deleteWs(wsid,wkstns)))
(SelRepresentation(wsid,pli,bl,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setrep(wsid,pli,bl,ndcp,wkstns)))
(SetView(wsid,vwn,omatrix,mmatrix,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setviewrep(wsid,vwn,omatrix,mmatrix,ndcp,wkstns))
   IF not (vwn==VWN0))
(SetViewSelCriterion(wsid,vwn,viewsel,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setviewsel(wsid,vwn,viewsel,ndcp,wkstns)))
(SetNDCVisualEffects(wsid,vefI,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setVeffects(wsid,vefI,ndcp,wkstns)))
(SetWSWindowandViewport(wsid,wsww,wsvw,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setwwandvw(wsid,wsww,wsvw,ndcp,wkstns)))
(SetWsSelCriterion(wsid,DISPLAY,sdis,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setsdis(wsid,ndcp,sdis,wkstns)))
(SetWsSelCriterion(wsid,HIGHLIGHTING,sh,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setsht(wsid,ndcp,sh,wkstns)))
(SetWsSelCriterion(wsid,DETECTABILITY,sd,mkGKS(gsI1,pps,ndcp,wkstns))
 = mkGKS(gsI1,pps,ndcp,setsd(wsid,ndcp,sd,wkstns)))

```

jbo

4. Conclusion

The specification presented here has been developed in parallel with the development of GKS-9x. During the course of the development, a number of omissions and ambiguities were found in the GKS-9x drafts, which were fed into the ISO/IEC review process as part of the UK comments on the drafts.

The specification has been executed using the ObjEx OBJ interpreter and test cases were used to explore the behaviour of the specification.

References

1. K.W. Brodlie, D.A. Duce, and F.R.A. Hopgood, "The New Graphical Kernel System," *Computer-Aided Design*, 1991.
2. L.B. Damnjanovic, D.A. Duce, and S.K. Robinson, "GKS-9x: Some Implementation Considerations," *Computer Graphics Forum*, vol. 12, no. 3, 1993. In press
3. L.B. Damnjanovic, D.A. Duce, and S.K. Robinson, "GKS-9x: Implementation of Selection," contained in ERCIM Research Reports ERCIM-93-R017, ERCIM, Domaine de Voluceau, Rocquencourt, B.P. 105, F-78153 Le Chesnay Cedex, France, 1993.
4. D.A. Duce, F.R.A. Hopgood, and K.W. Brodlie, "Revision of the Graphical Kernel System," *Proceedings of the Icographics '91 Conference*, 1991.
5. D.A. Duce and L.B. Damnjanovic, "Formal Specification in the Revision of GKS: An Illustrative Example," *Computer Graphics Forum*, vol. 11, no. 1, pp. 17-30, 1992.
6. D.A. Duce and F. Paterno, "A Formal Specification of a Graphics System in the Framework of the Computer Graphics Reference Model," *Computer Graphics Forum*, vol. 12, no. 1, pp. 3-20, 1993.
7. —, "Information processing systems - Computer graphics - Graphical Kernel System (GKS) functional description," ISO 7942, ISO Central Secretariat, August 1985.

8. —, "Information processing systems - Computer graphics - Programmer's Hierarchical Interactive Graphics System functional description," ISO/IEC 9592: 1, 1989.
9. —, "Information processing systems - Computer graphics - Computer Graphics Reference Model," ISO/IEC IS 11072, ISO Central Secretariat, In press.

