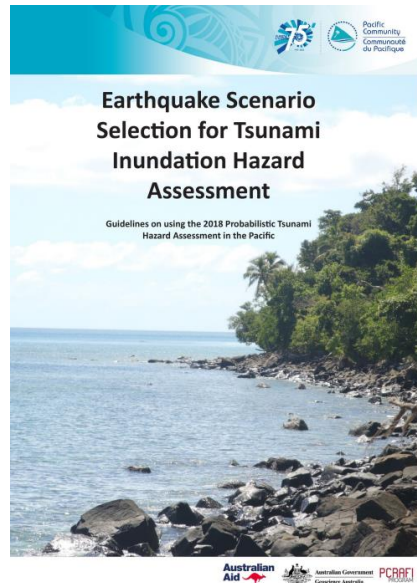
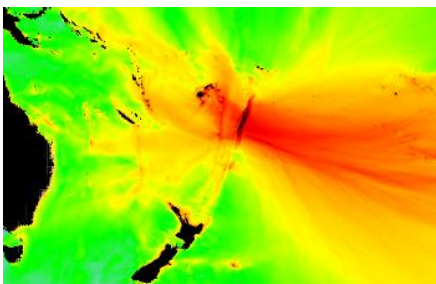
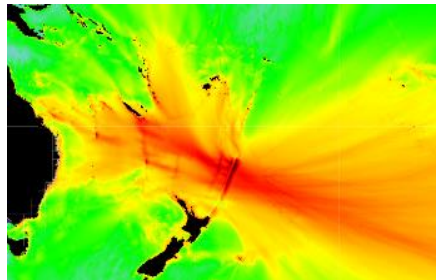
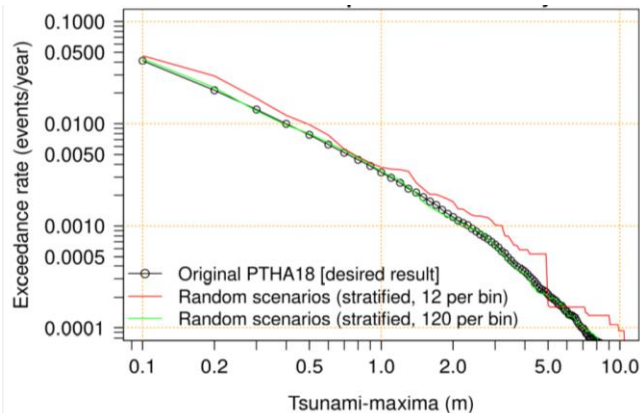




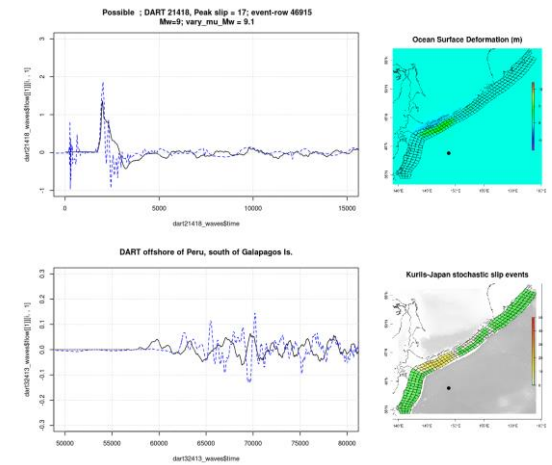
Earthquake scenario selection for tsunami inundation hazard assessment

Monte-Carlo techniques

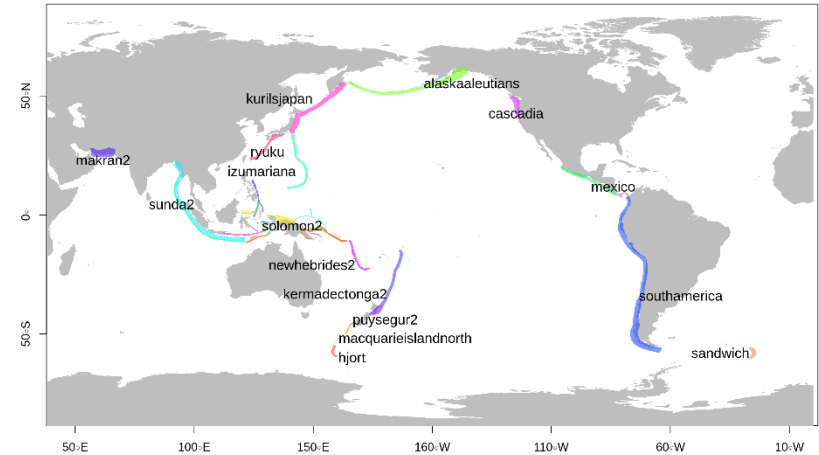
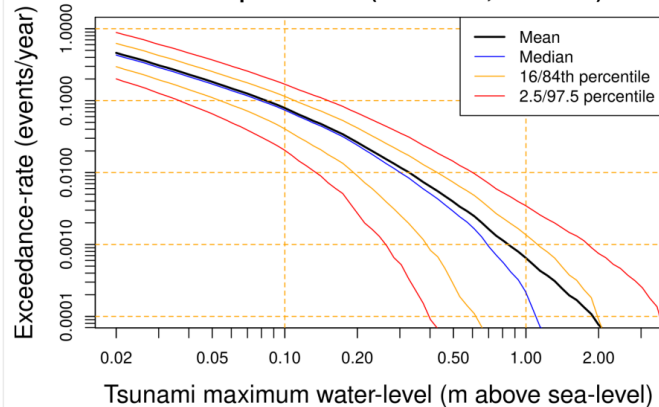


Reminder of the problem

- Offshore PTHA (earthquake-tsunami only)
 - Huge # of scenarios modelled in deep water
 - Scenario frequencies
 - Uncertainties in these frequencies



Modelled tsunami maximum water-level exceedance-rates
at a deep-ocean site (lon=158.45, lat=-15.66)



Reminder of the problem

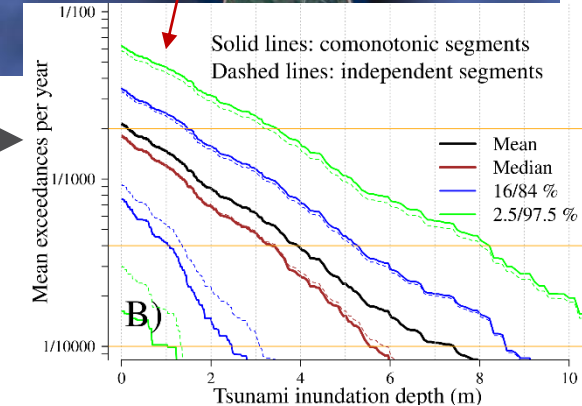
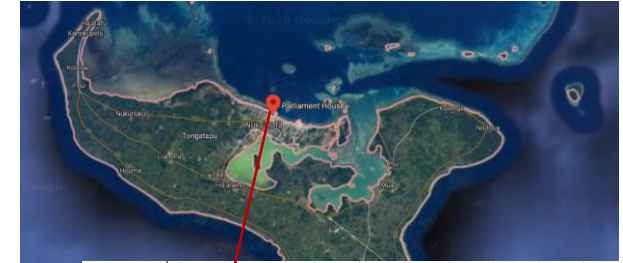
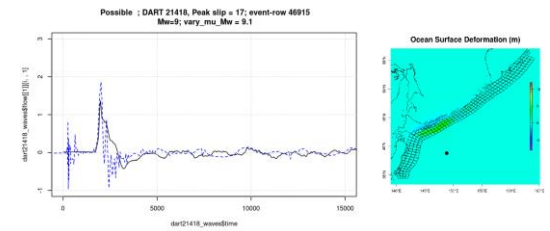
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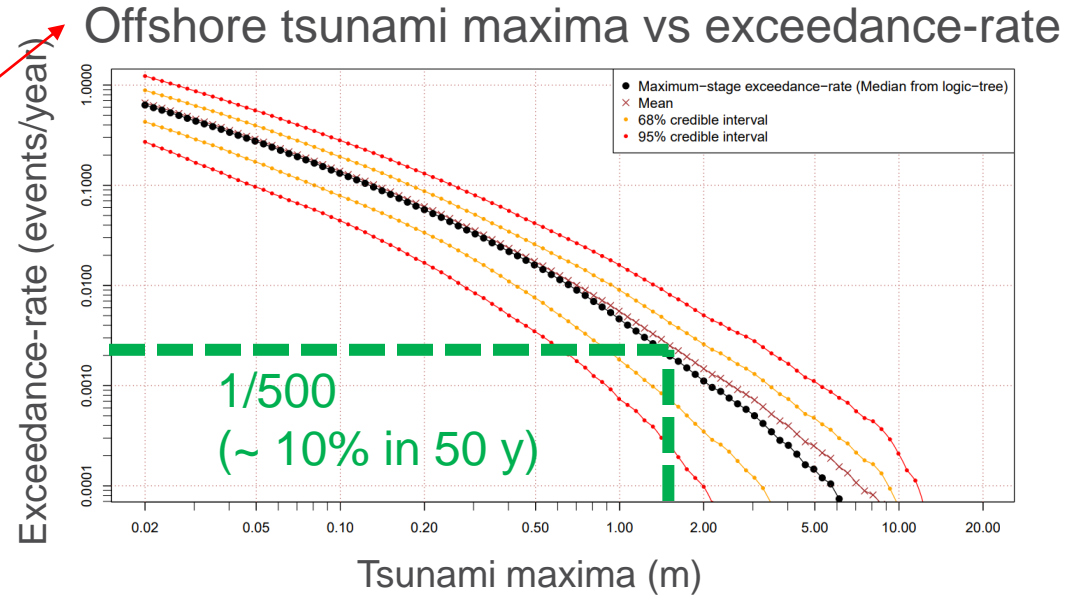
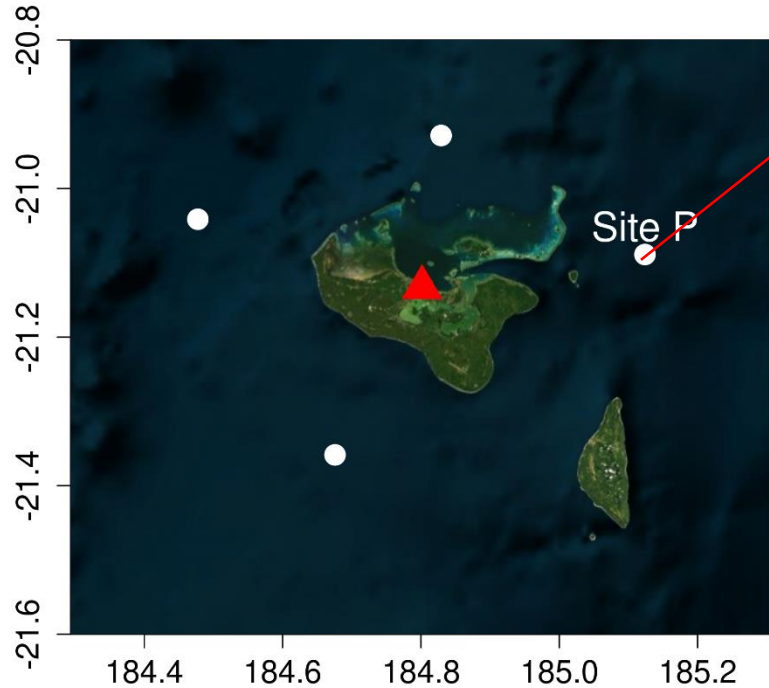
- Onshore hazard

- How big (e.g. depth at site of interest) ?
- How often (with uncertainty) ?
- Inundation computation is expensive
 - Cannot model all offshore PTHA scenarios

- Which scenarios should be used for onshore hazard assessment?

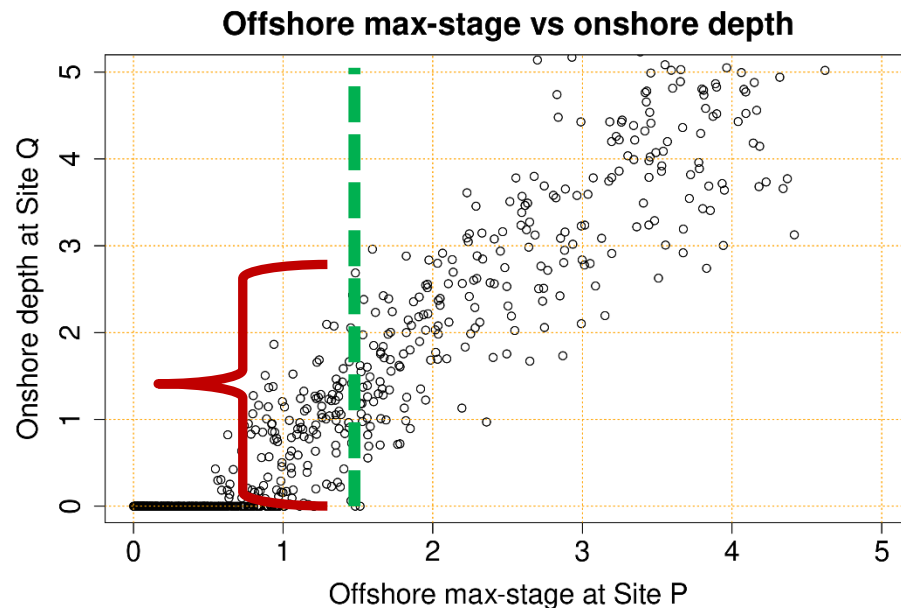
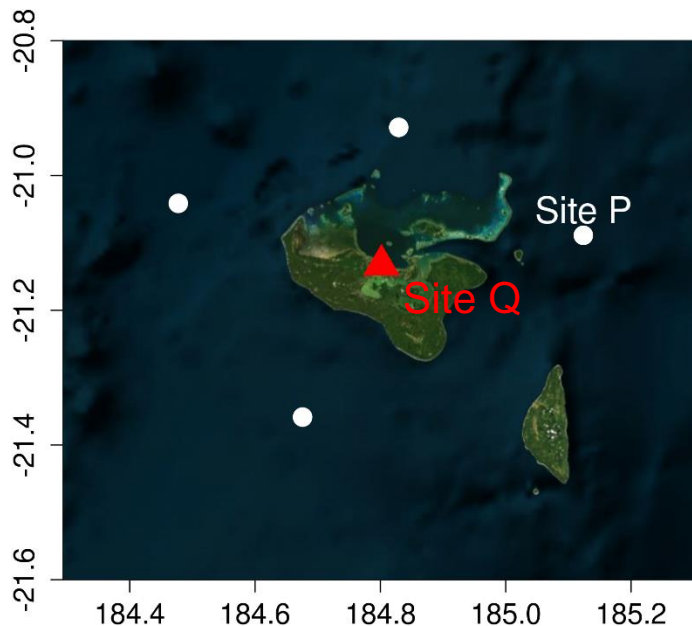


One approach: Find scenarios with offshore waves matching exceedance-rates of interest



Can offshore waves predict coastal impacts?

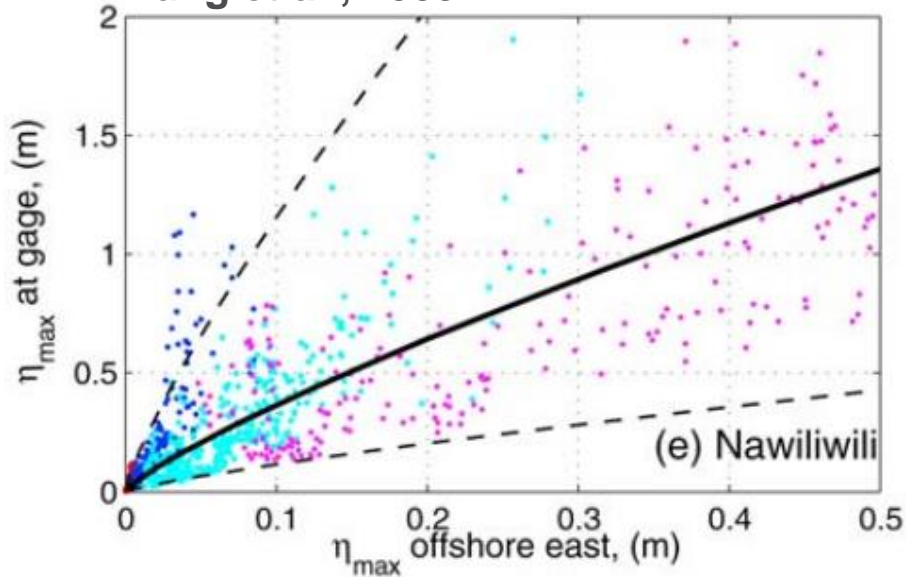
- Offshore waves are a rough predictor of nearshore & onshore waves
 - Normally there is lots of extra variability



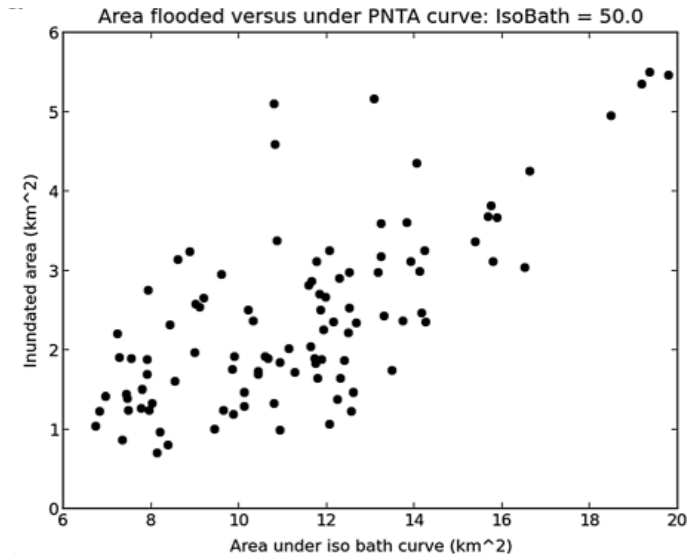
Can offshore waves predict coastal impacts?

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 - Normally there is lots of extra variability

Tang et al., 2009



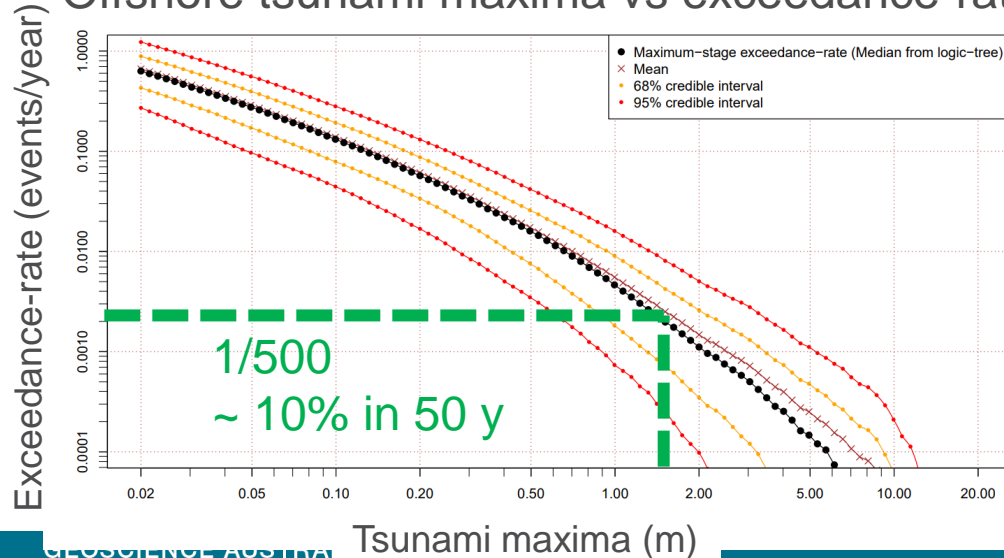
Mueller et al., 2015



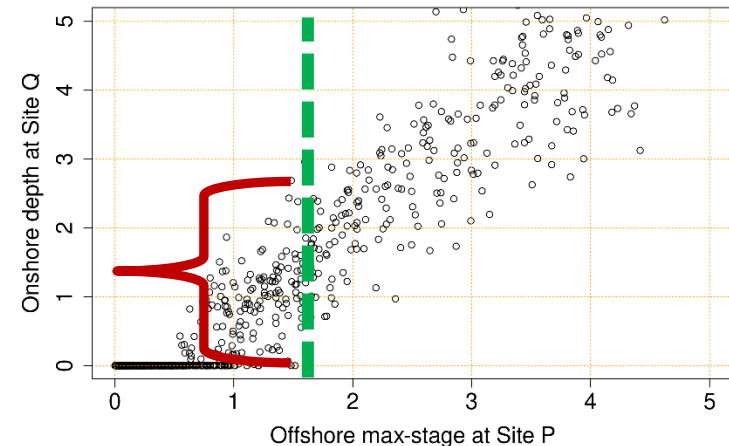
Can offshore waves predict coastal impacts?

- Offshore waves are a rough predictor of nearshore & onshore waves
- **Scenario return periods (from offshore sites) might not apply onshore**
 - 1/500 offshore wave \neq 1/500 depth onshore

Offshore tsunami maxima vs exceedance-rate



Offshore max-stage vs onshore depth



Can offshore waves predict coastal impacts?

- Offshore waves are a rough predictor of nearshore & onshore waves
- **Scenario return periods (from offshore sites) might not apply onshore**
 - 1/500 offshore wave \neq 1/500 depth onshore

Limitation of scenario-based approaches:

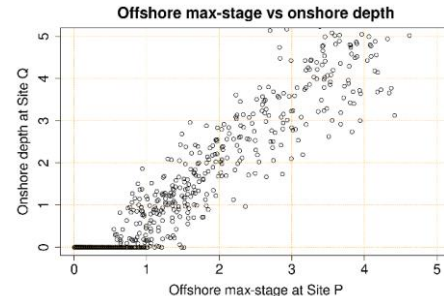
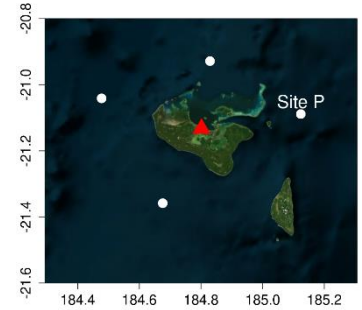
Even if we accept the accuracy of the:

☐ Offshore PTHA

☐ Inundation model

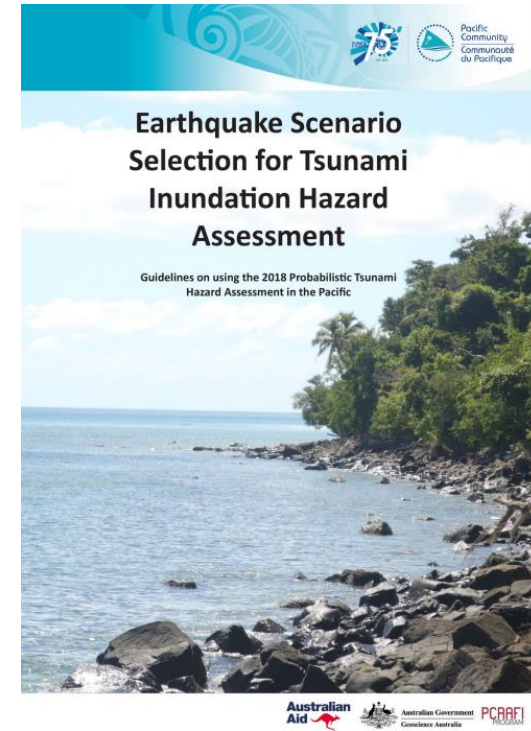
the onshore depths (and exceedance-rates) from scenario-based approach have limited precision

☐ Scenario variability



How should we use offshore PTHA for earthquake-tsunami inundation hazard assessment?

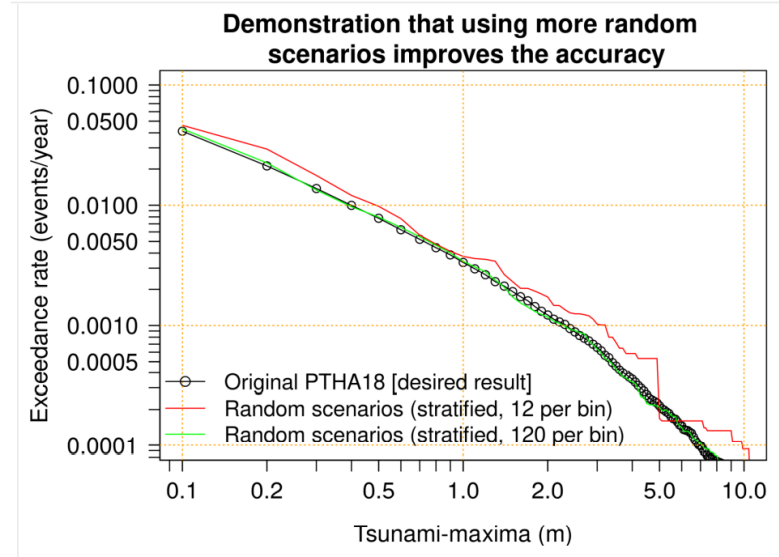
- More than one approach:
 1. **Multiple scenarios (Judith's presentation)**
 - Simple & computationally affordable
 - Not precise – but enough for many applications
 2. **All scenarios ?**
 - “Most accurate”
 - Unrealistic → Too computationally expensive
 3. **Monte-Carlo methods**
 - Approximate the “all scenarios” result
 - Fewer scenarios → more practical



Monte-Carlo methods for using offshore PTHA for inundation hazard assessment

The basic idea of Monte-Carlo methods

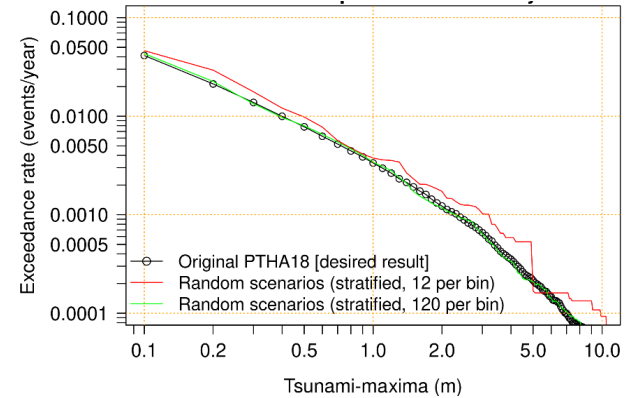
- “All scenarios” are approximated with a random subset of scenarios:
 - Hypothetical example
 - 100,000 scenarios (all)
 - Monte-Carlo approximation with 300 random scenarios
 - Inundation modelling feasible!
- **Has some error**
 - Can reduce using more scenarios
 - 3000 vs 300
 - Can reduce using better Monte Carlo methods



One common Monte-Carlo method

- Stratified-sampling by earthquake magnitude: **Often used in PTHA**

1. Group scenarios by magnitude
2. For each magnitude:
 - Sample N scenarios (w/ replacement)
 - Sampling weights \sim scenario-rates
3. Simulate inundation (random scenarios)
4. Estimate exceedance-rates



Converges to the “all-scenarios” solution (errors have variance $\sim 1/N$)

- Some error, unbiased

Much cheaper than simulating inundation for all scenarios

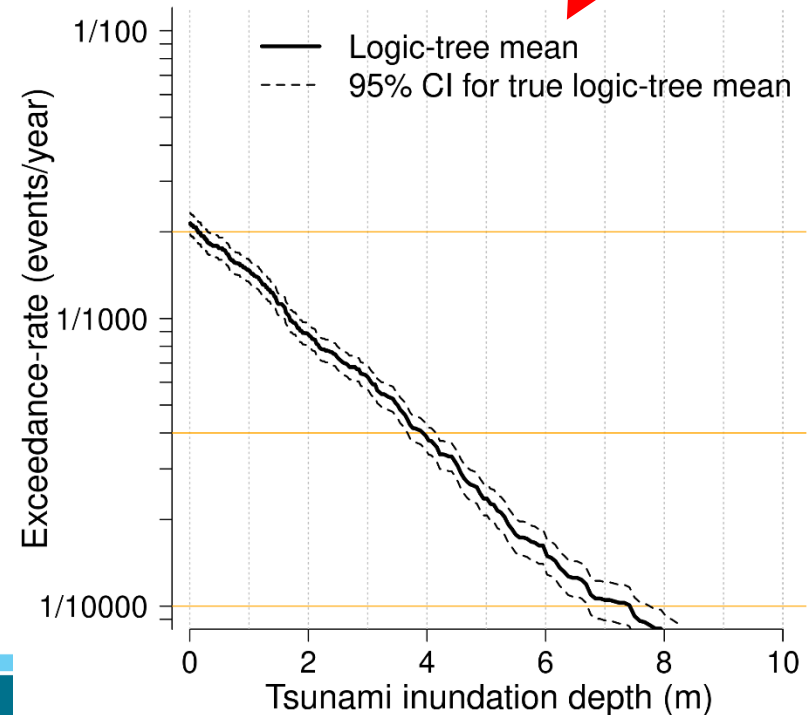
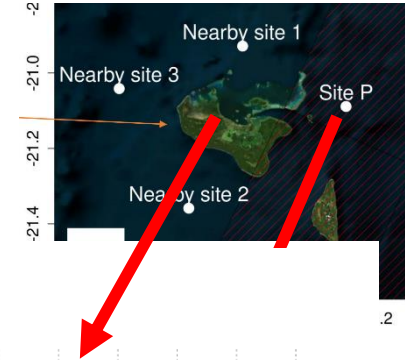
Useful properties of stratified-sampling for PTHA

- Offshore sites:

- Variance of Monte-Carlo errors can be computed analytically
- **No sampling required. Useful:**
 - Testing sampling schemes
 - Optimise non-uniform sampling of different magnitude bins

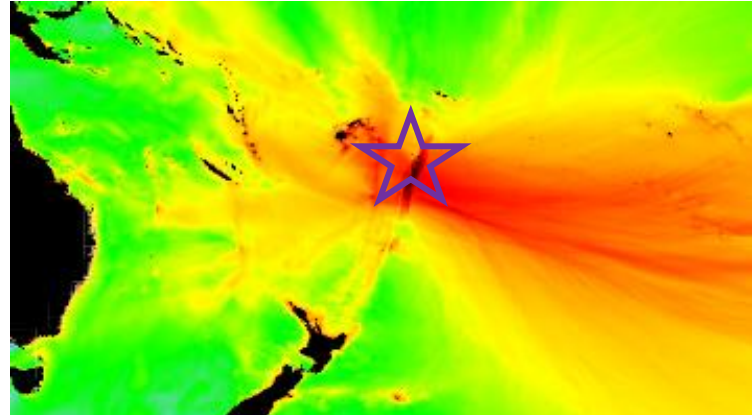
- Onshore sites:

- Variance of Monte-Carlo errors can be estimated from just one Monte-Carlo sample
 - Numerical reliability of onshore hazard

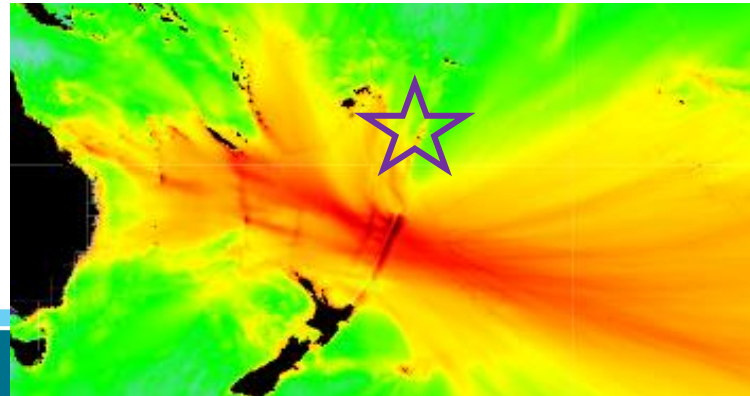


Weakness of stratified-sampling by magnitude

- *No influence of the tsunami size near site of interest*
 - But this is known in deep water (offshore PTHA)
 - Result: **Many scenarios with little inundation**
- **Example @ Tongatapu, Tonga**
 - Less than 25% of sampled scenarios with waves > 1m offshore nearby
 - Inefficient!

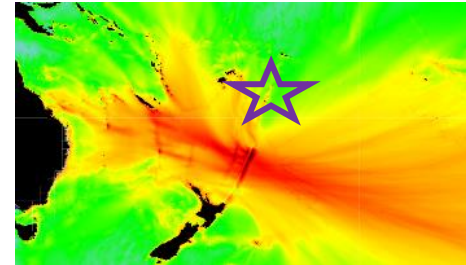
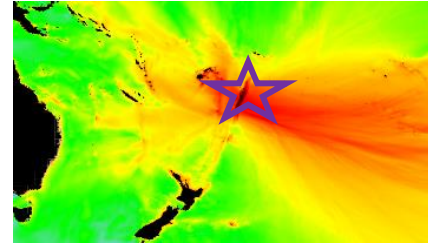


Two scenarios with magnitude 9.4



A solution: Modify the sampling to emphasise larger waves (*stratified/importance-sampling*)

1. Group scenarios by magnitude
2. For each magnitude:
 - **Biased sampling** of scenarios (w/ replacement)
 - Sampling weights \sim scenario-rates * (**wave height near our site**)
3. Simulate inundation (random scenarios)
4. Estimate exceedance-rates
 - Theory of importance-sampling \rightarrow unbiased

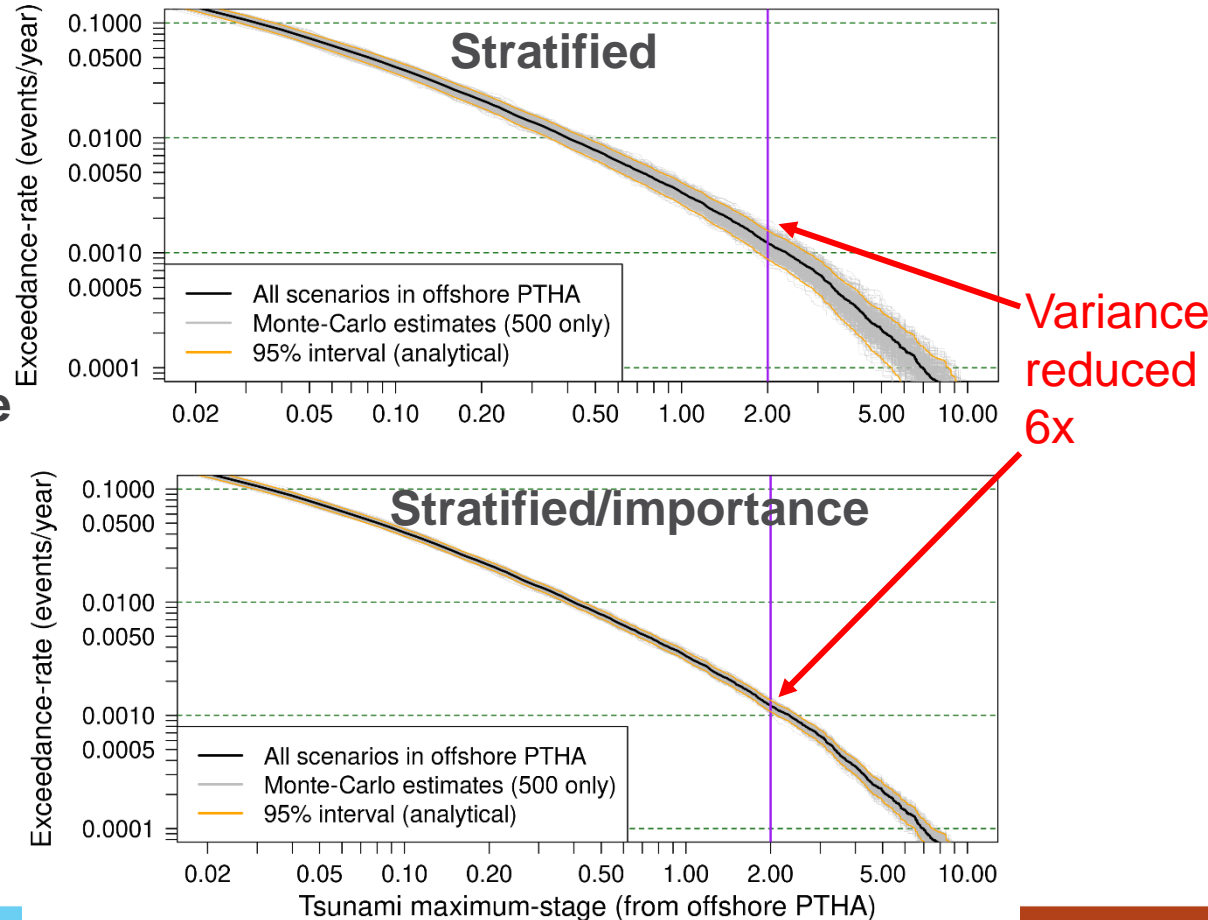
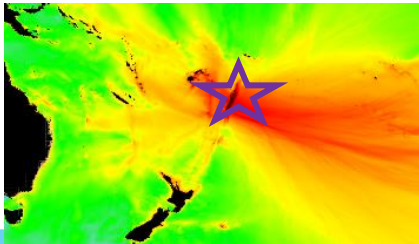


Better represents large tsunamis \rightarrow less Monte-Carlo error near our site

Shares all the other advantages of stratified-sampling

How much benefit?

- **Test at offshore site**
 - Both methods use 1200 scenarios
- **Strong reduction in Monte-Carlo error near the site of interest**

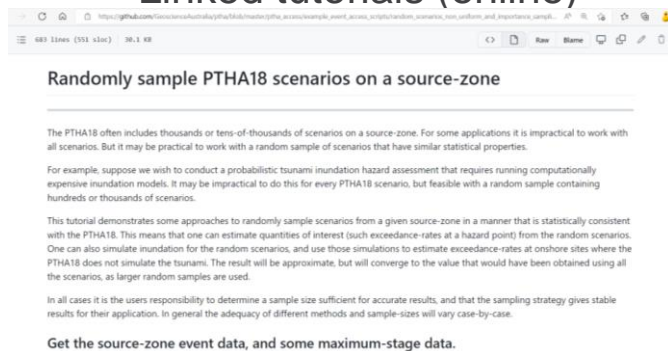


Resources to learn to how implement this

- Technical report

- <https://purl.org/spc/digilib/doc/dmup7>

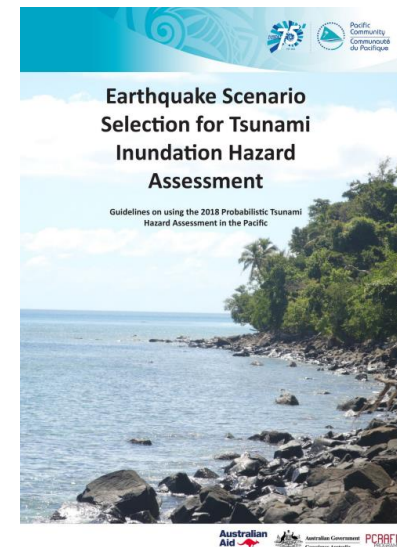
- Linked tutorials (online)



- Journal Paper:

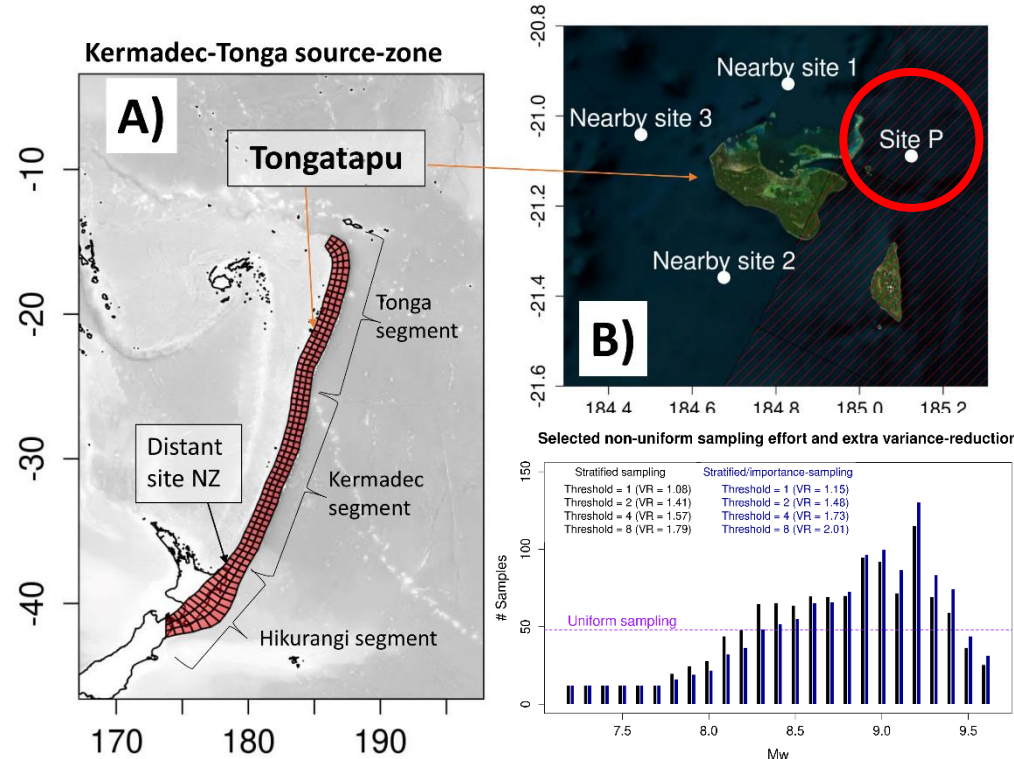
- <https://academic.oup.com/gji/article/230/3/1630/6566343>

- Associated code online



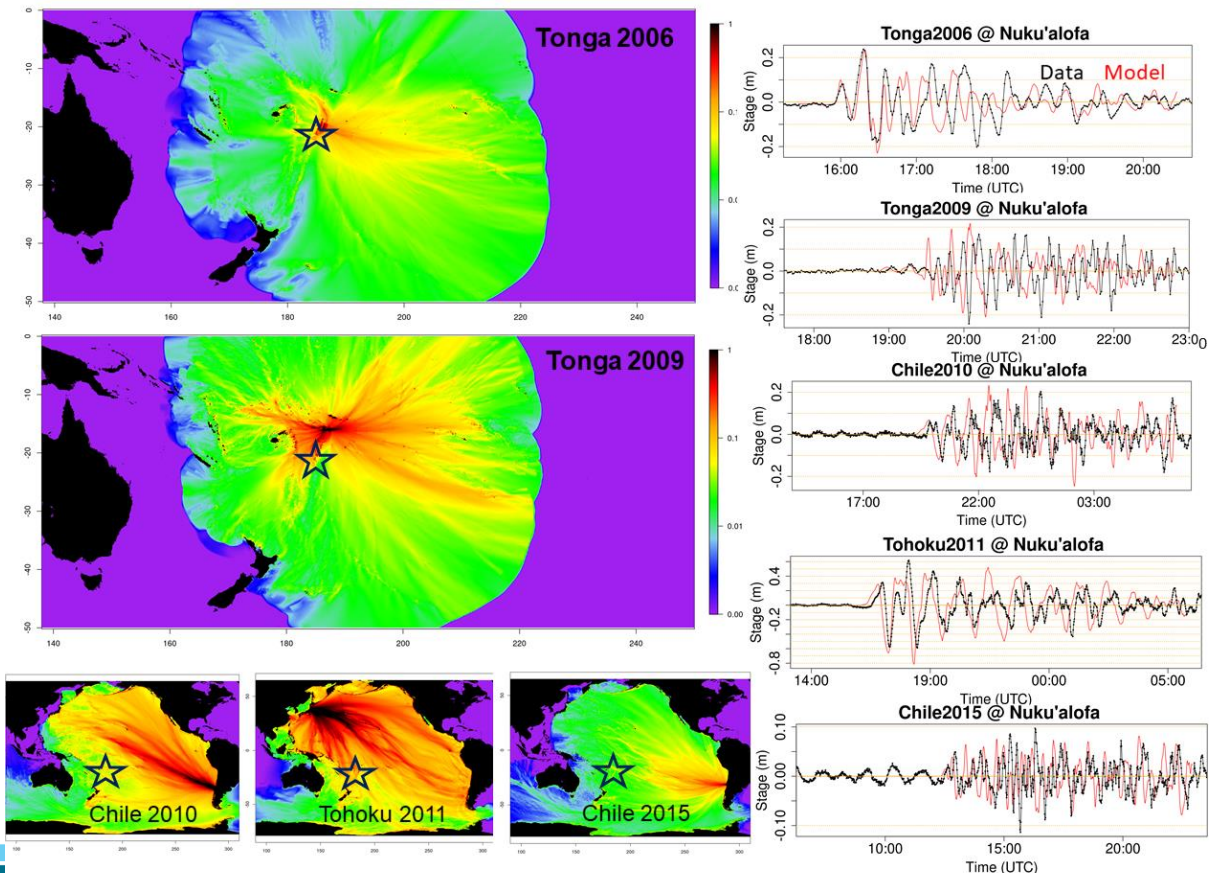
Application: Inundation Hazards @Tongatapu, Tonga

- 1200 random scenarios from Offshore PTHA
 - Stratified/importance sampling
 - Non-uniform sampling of magnitude-bins
- Initial testing of the Monte-Carlo performance offshore
 - Variance reduction by factor of 4 to 18 near Tongatapu
 - Compared to uniform stratified-sampling



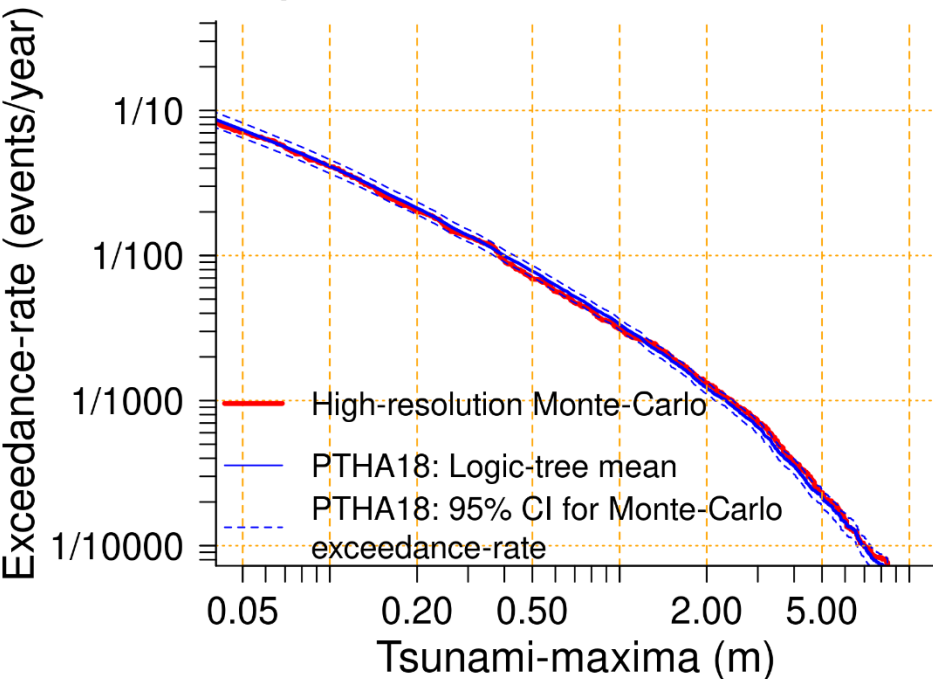
Application: Inundation Hazards @Tongatapu, Tonga

- Inundation model
 - Nonlinear shallow water equations (spherical)
 - 2-way nesting
 - 7.5 m grid-size onshore @ Tongatapu
- Tested against obs. of five historical tsunamis
 - Source models from offshore PTHA
- Simulated inundation for all random scenarios

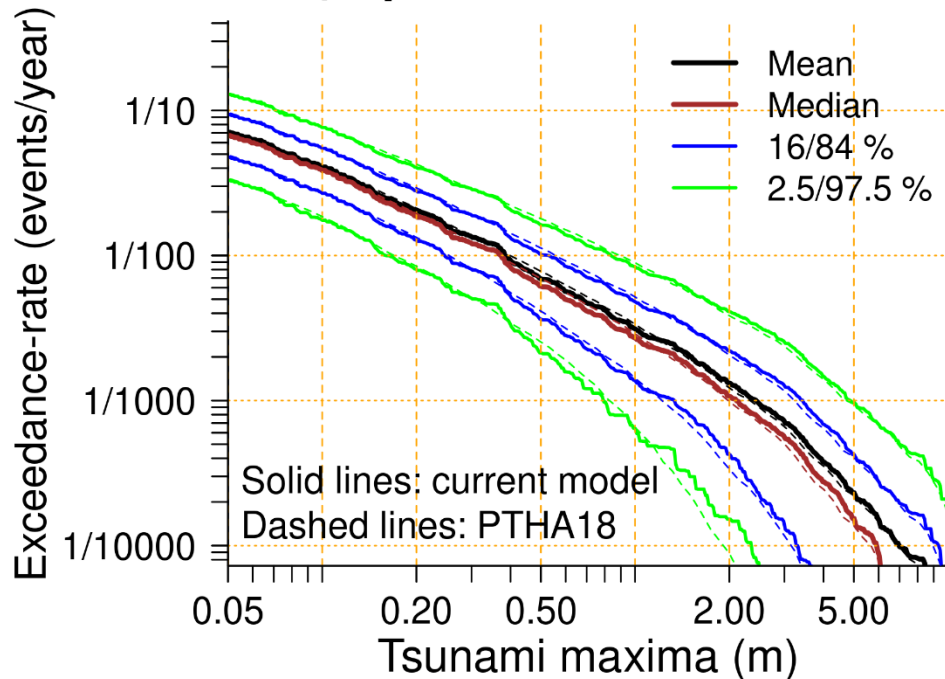


Sanity check: Do our results match PTHA18 offshore?

A) Monte-Carlo uncertainties

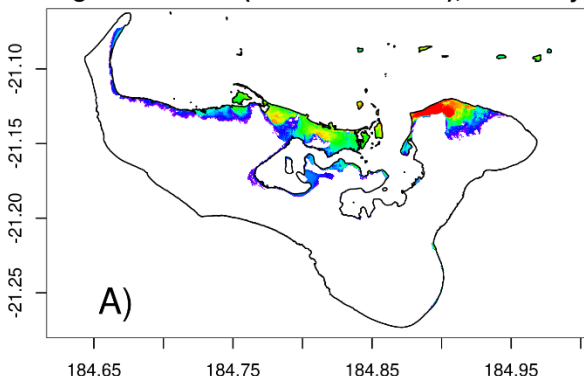


B) Epistemic uncertainties

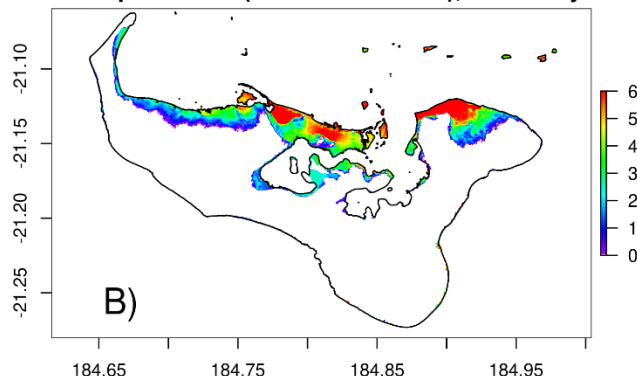


Results: Onshore hazards with quantified uncertainties

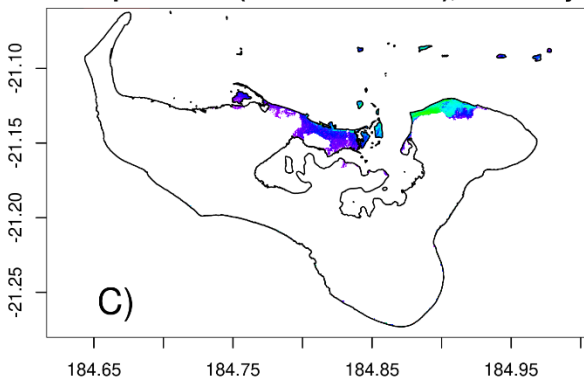
logic-tree mean (sea-level = 0.0 m), 2% in 50y



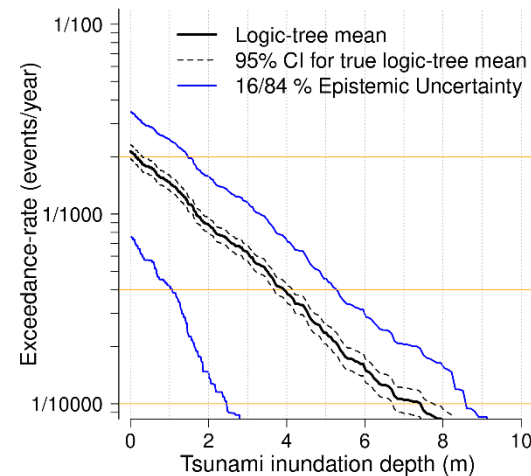
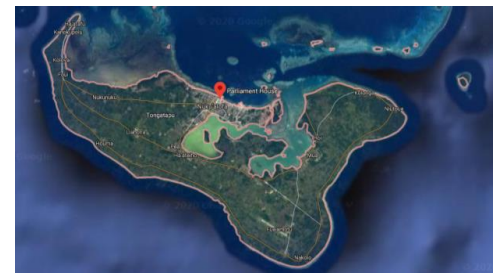
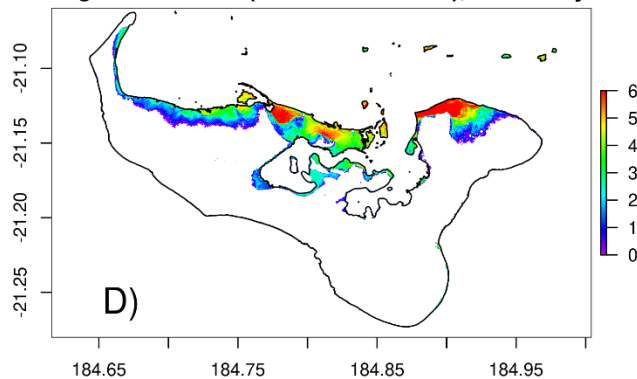
84th percentile (sea-level = 0.0 m), 2% in 50y



16th percentile (sea-level = 0.0 m), 2% in 50y

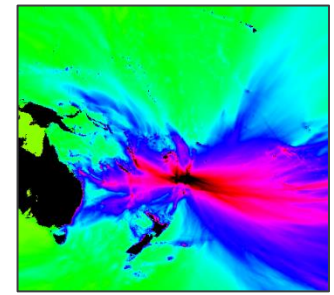


logic-tree mean (sea-level = 0.8 m), 2% in 50y

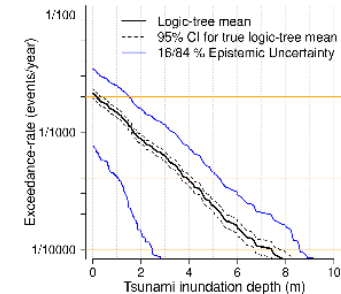
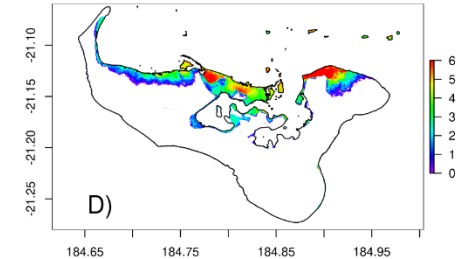


Summary

- How to transform offshore PTHA into onshore hazard?
 - Monte-Carlo methods provide one approach
 - Rigorous
 - Quantify uncertainties in the onshore hazard
 - Reflecting the offshore PTHA uncertainties
 - Tailor to particular site of interest for efficiency
- Downsides of Monte-Carlo approach:
 - More computationally expensive (vs scenario-based)
 - Is it worth it? Case-by-case decision.
 - Will the extra information be useful for your application?

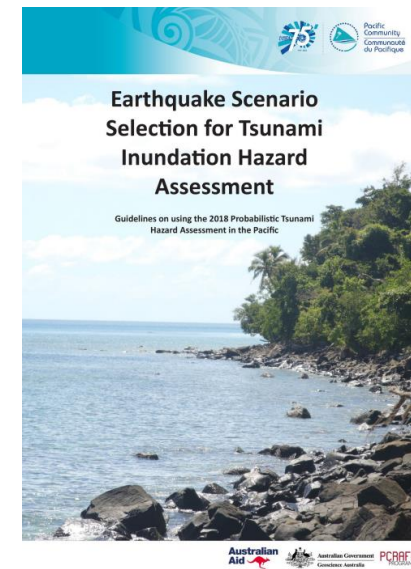
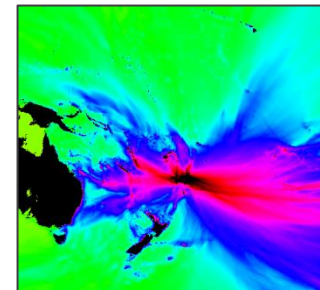


logic-tree mean (sea-level = 0.8 m), 2% in 50y



Don't forget the other limitations!

- Tsunamis are also generated by non-earthquake sources!
- Inundation models are not perfect!
- PTHA18 (and other offshore PTHAs) are not perfect!
 - Significant testing at global scales
 - Limited testing at your specific site.
 - Compare to other information
 - Paleotsunami, historical record
 - Expect the science to evolve over time.
- Yet our guidelines should (largely) be applicable to future offshore PTHAs





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